

Acceleration of particles in a plasma

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Course outline

- Last lectures:
 - Electron sources
 - Ion sources
- Today:
 - Acceleration in a plasma

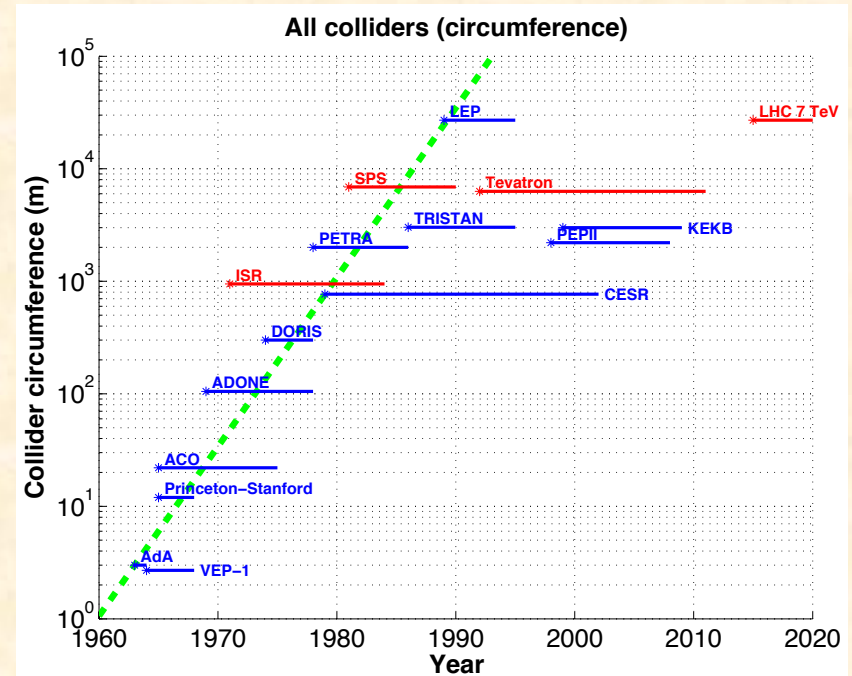
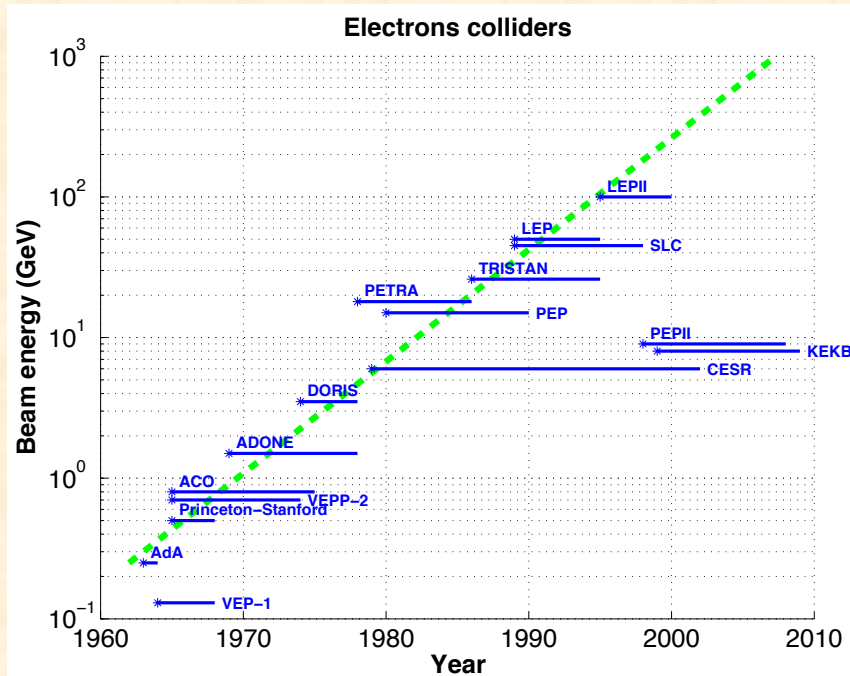
Plasma acceleration:

Content

- Motivation
- Acceleration of electrons in a plasma wakefield
 - Laser driven
 - Beam driven
- Acceleration of ions with a high power laser
 - The TNSA mechanism
 - Shock acceleration
- Most of the material shown here comes from the CAS School 2019 about plasma acceleration.

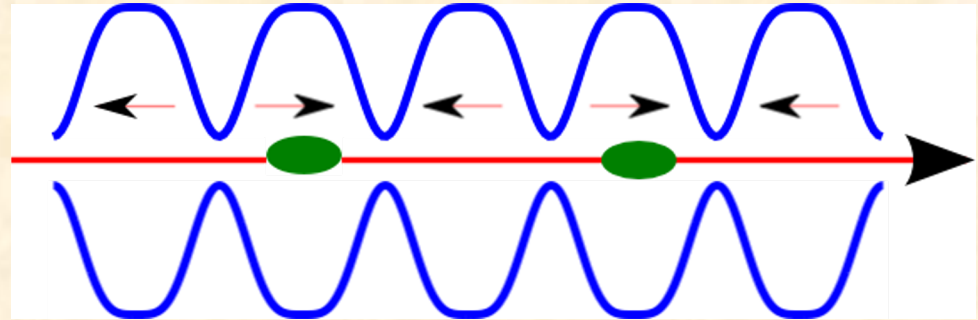
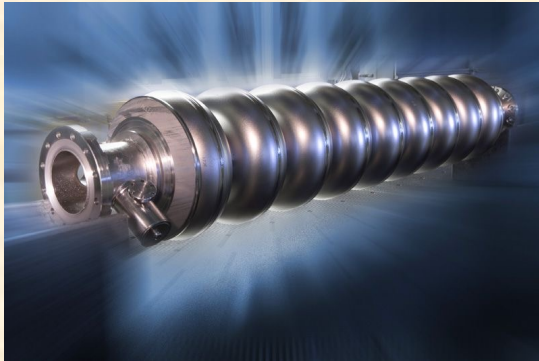
Motivations:

Limits of conventional technology



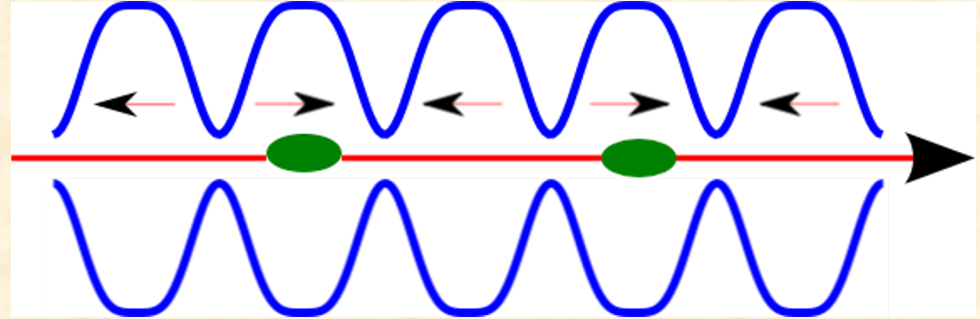
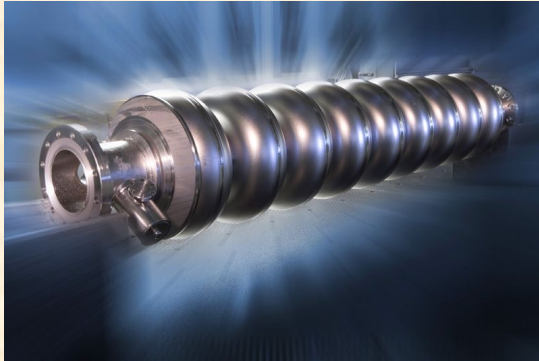
- Until 1995 the centre of mass energy of lepton colliders trebled every 6 years!
- Until 1989 lepton colliders doubled their circumference every 2 years!
- Since the start of LEP II in 1995 this trend has stopped.
- Conventional technologies no longer allow significant increases of colliders' centre of mass energy at the same pace.

Acceleration and RF frequency



- The highest the RF frequency, the higher the accelerating gradient will be.
- The ILC (and XFEL) operate in L-band at 1.3 GHz. Typical gradient $\sim 20\text{ MV/m}$ (maximum $\sim 35\text{ MV/m}$).
This corresponds to a wavelength of 23 cm.
- The LEP injector Linac (LIL) and several conventional accelerators operated in S-band at a frequency of 3 GHz. Typical gradient (now) $\sim 30\text{--}40\text{ MV/m}$.
This corresponds to a wavelength of 10 cm.
- CLIC considers operating in X-band at 12 GHz. Typical gradient $\sim 100\text{ MV/m}$.
This corresponds to a wavelength of 2,5 cm.
- Mechanical realisation becomes more and more difficult.
- Can we do without a cavity with high frequency RF waves?

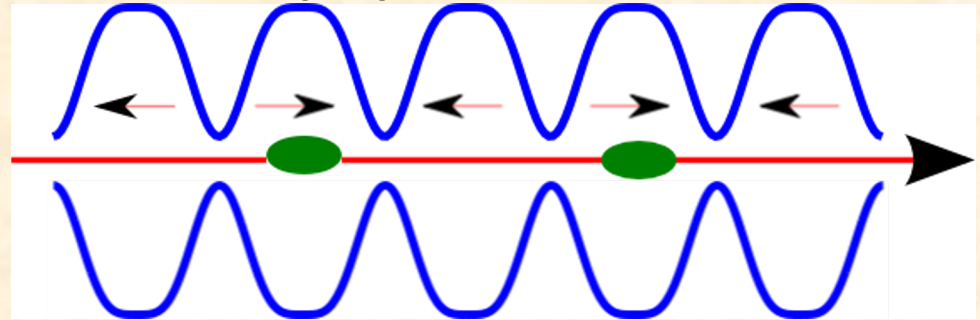
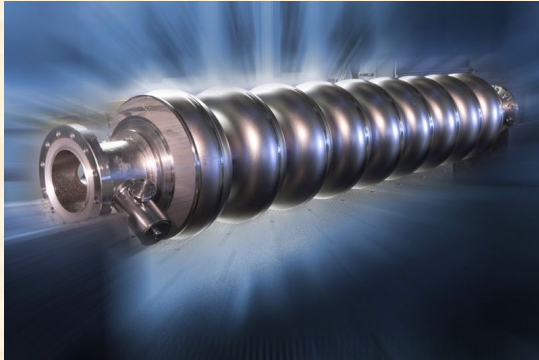
Quizz



- What is the frequency of optical light (500nm)?
- (a) 12GHz
- (b) 100 MHz
- (c) 600THz
- (d) 3 THz

Quizz

Answer: (C)



- What is the frequency of optical light (500nm)?
- $3\text{GHz} \Rightarrow 100\text{mm}$, $50\text{mm} \Rightarrow 6\text{GHz}$, $50\text{nm} \Rightarrow 6\text{PHz}$, $500\text{nm} \Rightarrow 600\text{THz}$
- (a) 12GHz
- (b) 100 MHz
- (c) 600THz

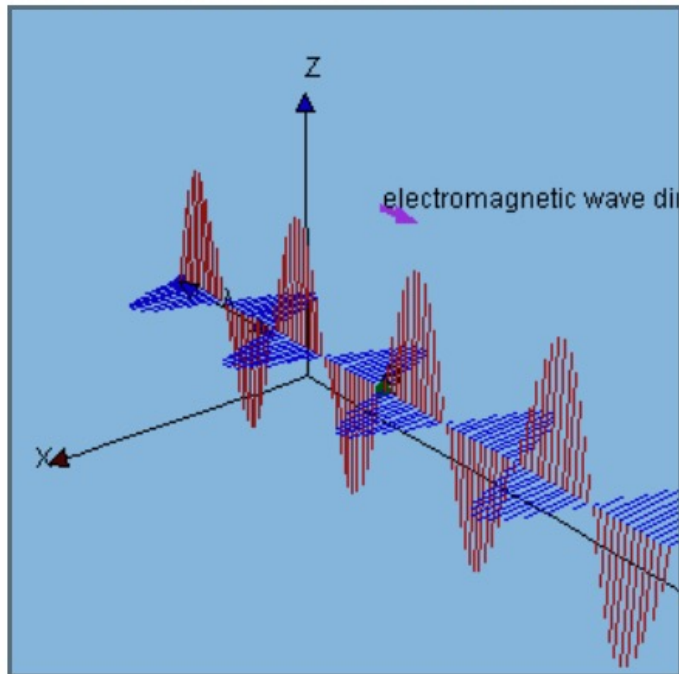
Lawson-Woodward Theorem

(J.D. Lawson, IEEE Trans. Nucl. Sci. NS-26, 4217, 1979)

The net energy gain of a relativistic electron interacting with an electromagnetic field **in vacuum** is zero.

The theorem assumes that

- (i) the laser field is in vacuum with no walls or boundaries present,
- (ii) the electron is highly relativistic ($v \approx c$) along the acceleration path,
- (iii) no static electric or magnetic fields are present,
- (iv) the region of interaction is infinite,



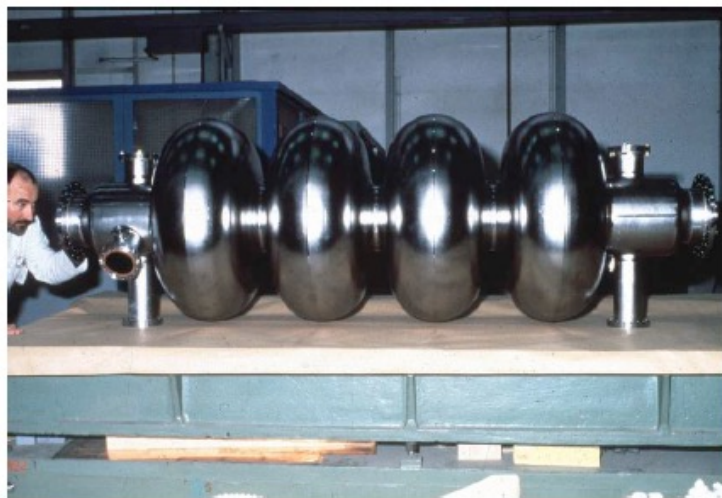
$$\Delta\mathcal{E} = e \int_{-\infty}^{\infty} \mathbf{v} \cdot \mathbf{E}(\mathbf{r}(t), t) dt, \quad \mathbf{r}(t) = \mathbf{r}_0 + \mathbf{v}t,$$

$$\mathbf{E}(\mathbf{r}, t) = \int d^3k \tilde{\mathbf{E}}(\mathbf{k}) e^{i\mathbf{k} \cdot \mathbf{r} - i\omega t}, \quad \omega = ck.$$

$$\begin{aligned} \Delta\mathcal{E} &= e\mathbf{v} \cdot \int_{-\infty}^{\infty} dt \int d^3k \tilde{\mathbf{E}}(\mathbf{k}) e^{i\mathbf{k} \cdot (\mathbf{r}_0 + \mathbf{v}t) - i\omega t} \\ &= 2\pi e \int d^3k \mathbf{v} \cdot \tilde{\mathbf{E}}(\mathbf{k}) e^{i\mathbf{k} \cdot \mathbf{r}_0} \delta(\omega - \mathbf{k} \cdot \mathbf{v}) \equiv 0 \end{aligned}$$

$$\omega - \mathbf{k} \cdot \mathbf{v} = ck(1 - \beta \cos \alpha) > 0, \Rightarrow \delta \equiv 0$$

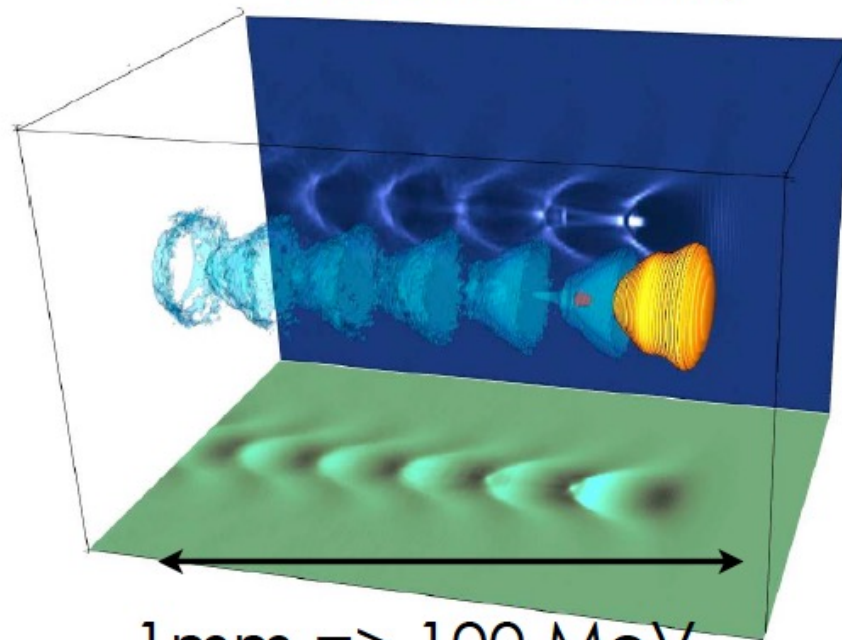
RF Cavity



1 m \Rightarrow 50 MeV Gain

Electric field < 100 MV/m

Plasma Cavity



1 mm \Rightarrow 100 MeV

Electric field > 100 GV/m

V. Malka *et al.*, Science **298**, 1596 (2002)

Frequency in plasma

- Remember the characteristic oscillation frequency in a plasma:

$$\omega_e = \sqrt{\frac{e^2 n}{\epsilon_0 m_e}}$$

- For 10^{17} e-/cm³ this gives ~ 3 THz
- Wavelength $\sim 100\mu\text{m}$
- In an under dense plasma higher frequencies can be reached
=> higher accelerating gradients.

Quizz:

Frequency in plasma

- What is the optical wavelength corresponding to 3 THz?
 - (a) 500nm
 - (b) 100um
 - (c) 500um

Quizz:

Answer (b)

- What is the optical wavelength corresponding to 3 THz?

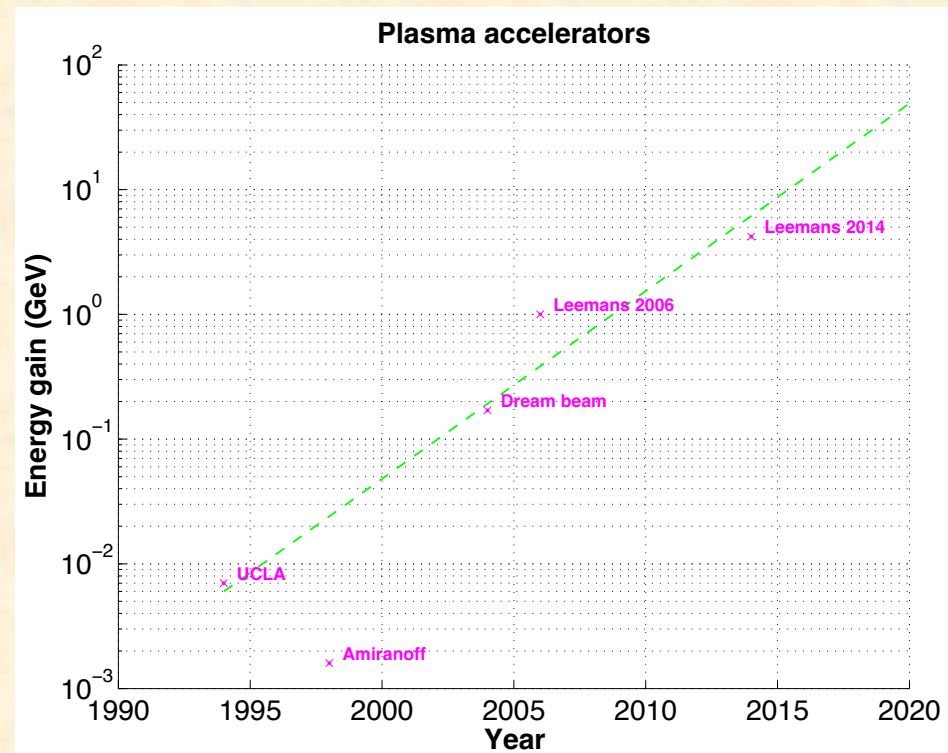
~~(a) 500nm~~

(b) 100μm (3GHz \Leftrightarrow 100mm \Rightarrow 3THz \Leftrightarrow 100μm)

~~(c) 500μm~~

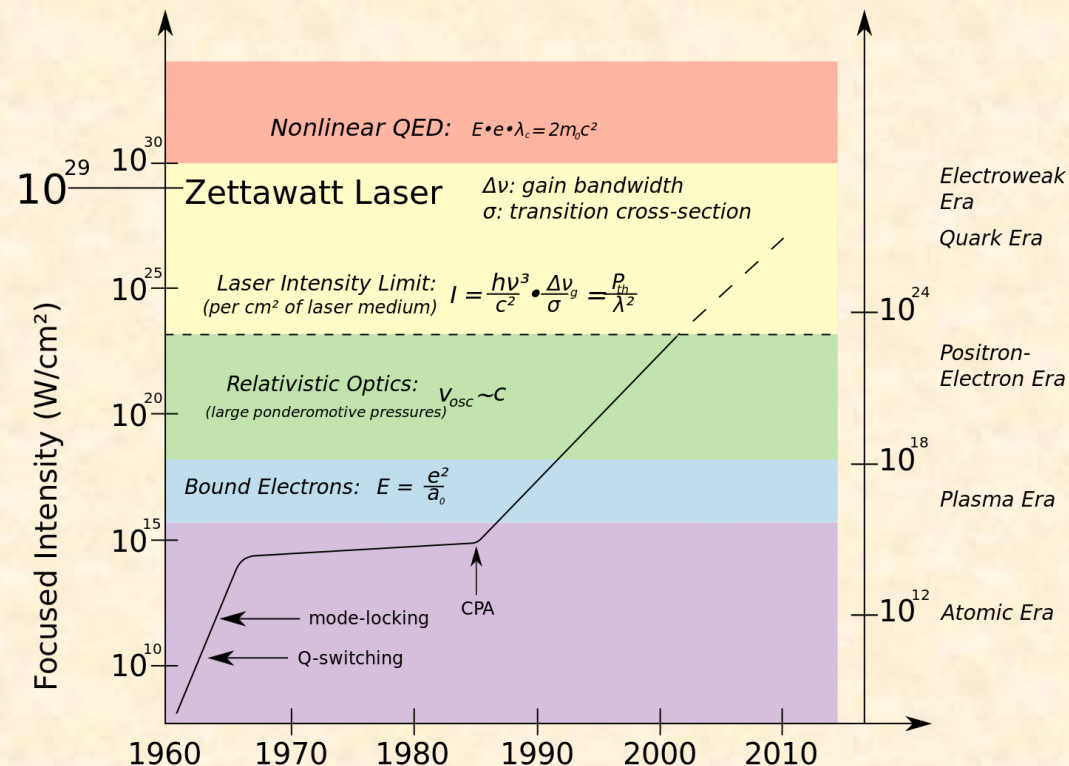
Are laser-plasma accelerators the answer?

- Laser-plasma accelerators double the maximum energy reached every two years!
- Beware: this is the maximum energy of some particles in the beam, not the beam energy and not the energy available for HEP collisions.
- This doubling is (mostly) driven by increases in laser-power.
- Such beams are still rather unstable. They have a low charge and high dispersion with respect to what can be achieved in conventional accelerators.

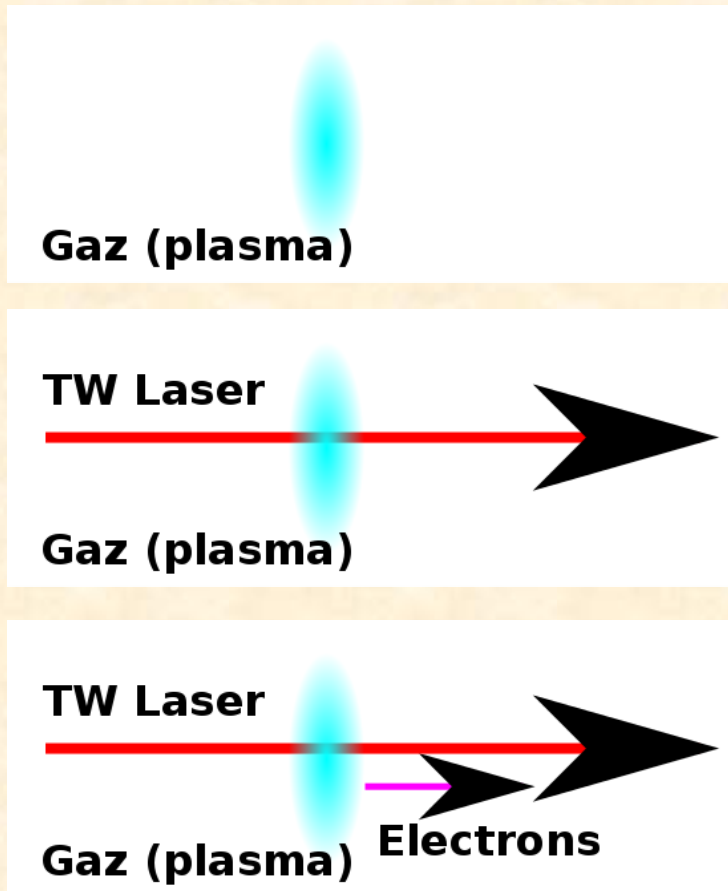


Lasers still have a significant margin for improvement.

- Laser technology is still improving significantly.
- Fibre lasers have more and more applications with a good efficiency and they have not yet reached the “high power” range.

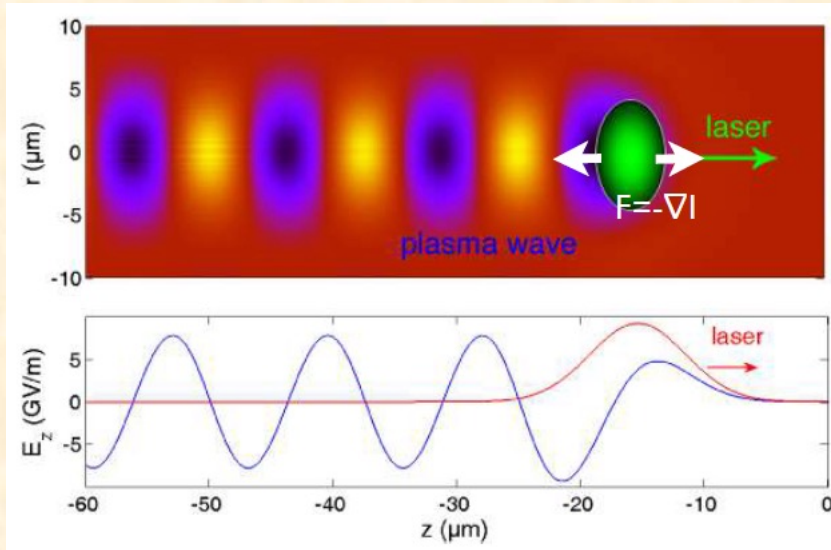


Principle of an experiment of electron acceleration in a plasma



- A gas volume (at low density/pressure: \sim mbar) will be used to create the plasma.
- This volume is ionised by a beam (laser, particles) at high power and ultra-short (duration: ps, fs).
- Electrons coming either from the plasma or from an external source will be captured and accelerated.
- The size of the “cavities” is of the order of a few hundred micrometres.

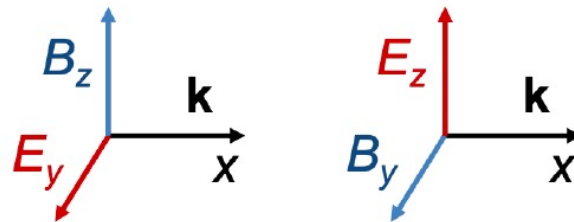
Principle of an experiment of electron acceleration in a plasma



- A gas volume (at low density/pressure: $\sim \text{mbar}$) will be used to create the plasma.
- This volume is ionised by a beam (laser, particles) at high power and ultra-short (duration: ps, fs).
- Electrons coming either from the plasma or from an external source will be captured and accelerated.
- The size of the “cavities” in the wake of the laser is of the order of a few hundred micrometres.
- GV/m gradients can be reached with $\sim 10^{18} \text{ e}^-/\text{cm}^3$ ($\sim 20 \text{ mbar}$).

Electron dynamics in a plasma

Electromagnetic plane waves



Transverse EM wave can be described by general, elliptically polarized vector potential $\mathbf{A}(\omega, \mathbf{k})$ travelling in the positive x -direction:

$$\mathbf{A} = A_0(0, \delta \cos \phi, (1 - \delta^2)^{\frac{1}{2}} \sin \phi), \quad (16)$$

where $\phi = \omega t - kx$ is the phase of the wave; A_0 its amplitude ($v_{os}/c = eA_0/mc$) and δ the polarization parameter :

- $\delta = \pm 1, 0 \rightarrow$ linear pol.: $\mathbf{A} = \pm \hat{\mathbf{y}} A_0 \cos \phi; \quad \mathbf{A} = \hat{\mathbf{z}} A_0 \sin \phi$
- $\delta = \pm \frac{1}{\sqrt{2}} \rightarrow$ circular pol.: $\mathbf{A} = \frac{A_0}{\sqrt{2}} (\pm \hat{\mathbf{y}} \cos \phi + \hat{\mathbf{z}} \sin \phi)$

Courtesy of Paul Gibbon, CAS 2019

Solution recipe

Bardsley et al., Phys. Rev. A 40, 3823 (1989)

Hartemann et al., Phys. Rev. E 51, 4833 (1995)

- 1 Laser fields $\mathbf{E} = -\partial_t \mathbf{A}$, $\mathbf{B} = \nabla \times \mathbf{A}$
- 2 Use dimensionless variables such that
 $\omega = k = c = e = m = 1$
(eg: $\mathbf{p} \rightarrow \mathbf{p}/mc$, $\mathbf{E} \rightarrow e\mathbf{E}/m\omega c$ etc.)
- 3 First integrals give conservation relations:
 $\mathbf{p}_\perp = \mathbf{A}$, $\gamma - p_x = \alpha$, where $\gamma^2 - p_x^2 - p_\perp^2 = 1$; $\alpha = \text{const.}$
- 4 Change of variable to wave phase $\phi = t - x$
- 5 Solve for $\mathbf{p}(\phi)$ and $\mathbf{r}(\phi)$

Courtesy of Paul Gibbon, CAS 2019

Plasma acceleration

Solution: *laboratory* frame

Lab frame: the electron initially at rest before the EM wave arrives, so that at $t = 0$, $p_x = p_y = 0$ and $\gamma = \alpha = 1$.

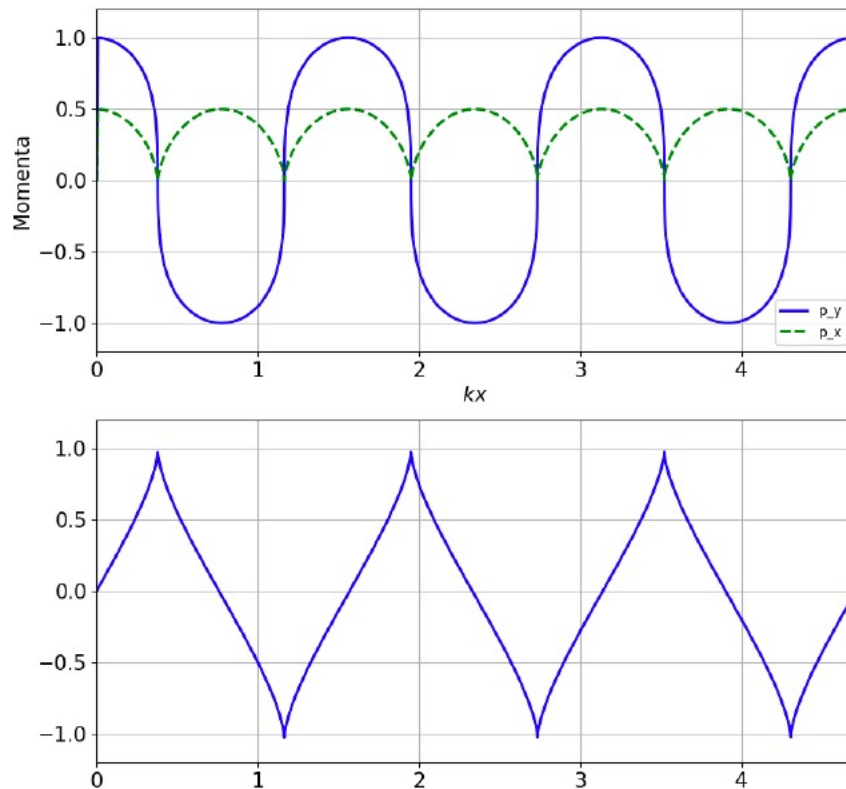
$$\begin{aligned} p_x &= \frac{a_0^2}{4} [1 + (2\delta^2 - 1) \cos 2\phi] , \\ p_y &= \delta a_0 \cos \phi, \\ p_z &= (1 - \delta^2)^{1/2} a_0 \sin \phi. \end{aligned} \tag{19}$$

Integrate again to get trajectories:

$$\begin{aligned} x &= \frac{1}{4} a_0^2 \left[\phi + \frac{2\delta^2 - 1}{2} \sin 2\phi \right] , \\ y &= \delta a_0 \sin \phi, \\ z &= -(1 - \delta^2)^{1/2} a_0 \cos \phi. \end{aligned} \tag{20}$$

NB: solution is *self-similar* in the variables $(x/a_0^2, y/a_0, z/a_0)$

Linearly polarized wave ($\delta = 1$)



Electron *drifts* with average momentum

$$p_D \equiv \overline{p_x} = \frac{a_0^2}{4},$$

or velocity

$$\frac{v_D}{c} = \overline{v_x} = \frac{\overline{p_x}}{\gamma} = \frac{a_0^2}{4 + a_0^2}$$

Single electron motion in EM plane wave

Electron momentum in electromagnetic wave with fields \mathbf{E} and \mathbf{B} given by Lorentz equation (SI units):

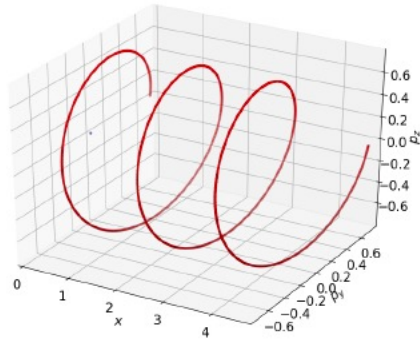
$$\frac{d\mathbf{p}}{dt} = -e(\mathbf{E} + \mathbf{v} \times \mathbf{B}), \quad (17)$$

with $\mathbf{p} = \gamma m \mathbf{v}$, and relativistic factor $\gamma = (1 + p^2/m^2 c^2)^{\frac{1}{2}}$.

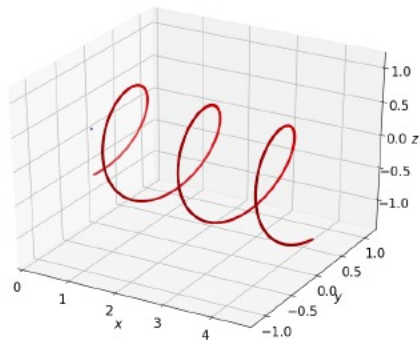
This has an associated energy equation, after taking dot product of \mathbf{v} with Eq. (17):

$$\frac{d}{dt} (\gamma m c^2) = -e(\mathbf{v} \cdot \mathbf{E}), \quad (18)$$

Circularly polarized wave ($\delta = \pm 1/\sqrt{2}$)



Oscillating p_x component at 2ϕ vanishes, but drift p_D remains.

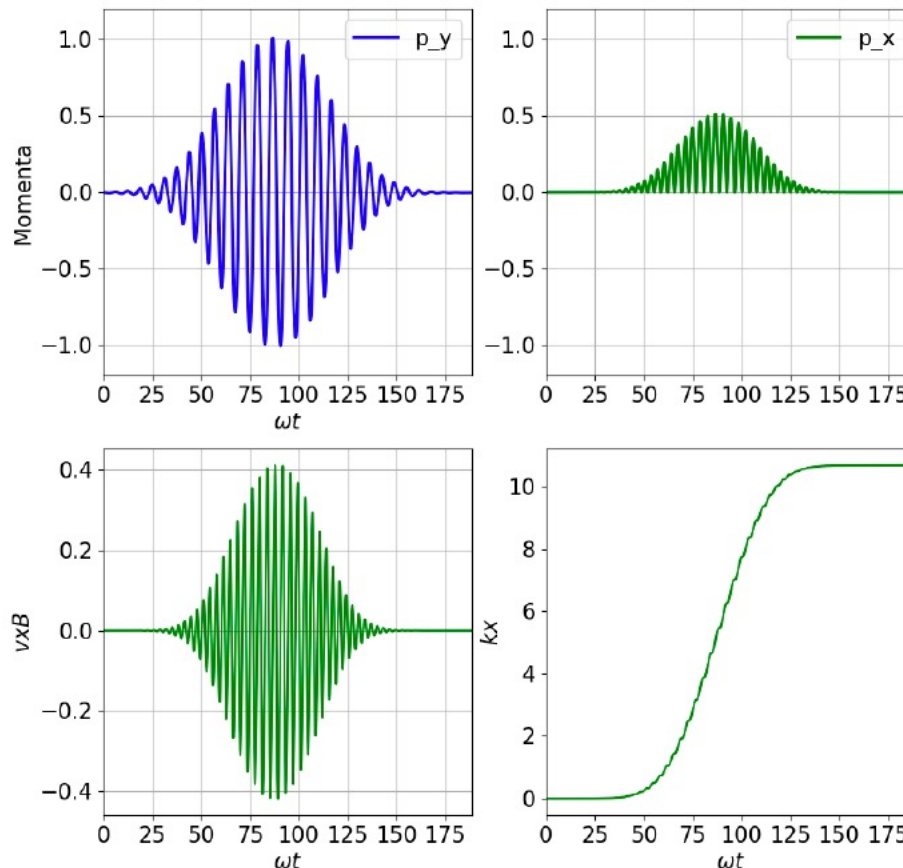


Orbit is *Helix* with:

- radius $kr_{\perp} = a_0/\sqrt{2}$
- momentum $p_{\perp}/mc = a_0/\sqrt{2}$
- pitch angle $\theta_p = p_{\perp}/p_D = \sqrt{8}a_0^{-1}$

Finite pulse duration - LP

Longitudinal Polarization



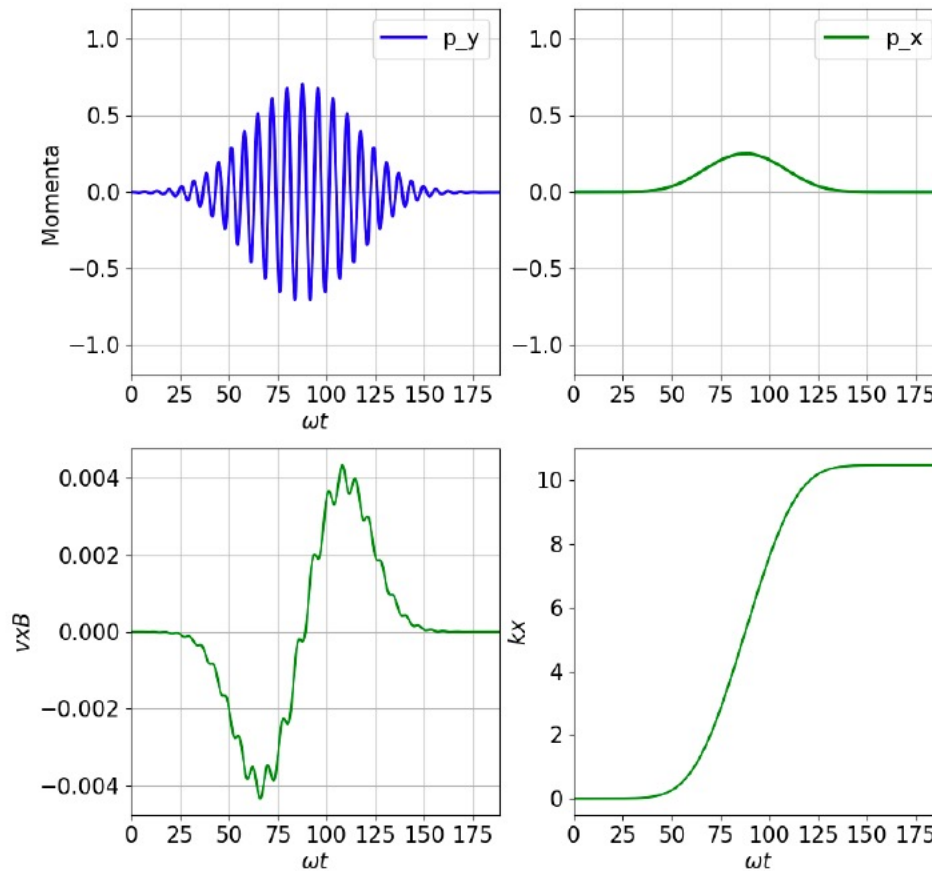
Pulse with
temporal envelope
in the wave vector
Eq. (16).

$$\mathbf{A}(x, t) = f(t) a_0 \cos \phi,$$

No net energy
gain!
Lawson-Woodward
theorem

Courtesy of Paul Gibbon, CAS 2019
Plasma acceleration

Finite pulse duration - CP Circular Polarization



No oscillations in p_x , but drift still there.

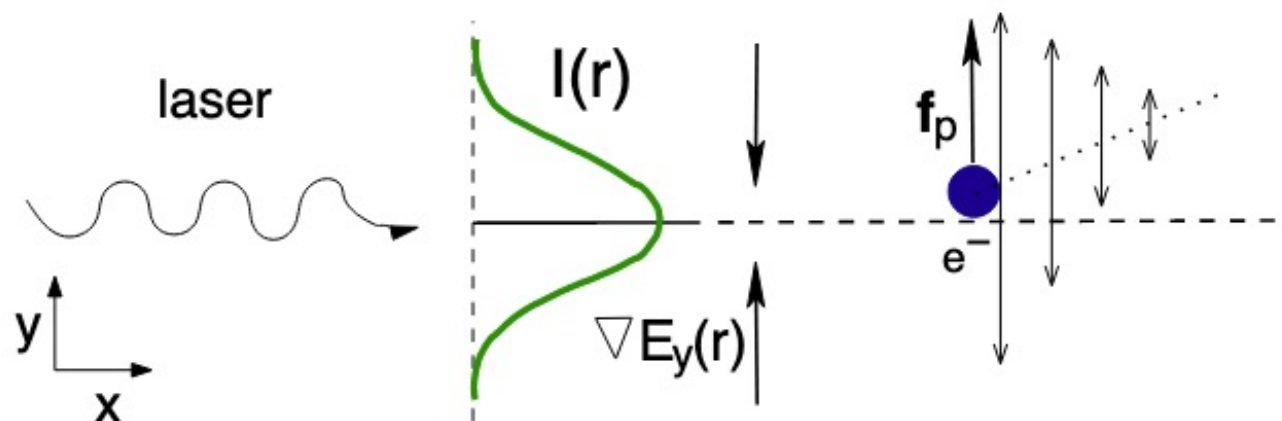
$v \times B$ oscillations also nearly vanish, but 'DC' part retained:

longitudinal ponderomotive force!

Courtesy of Paul Gibbon, CAS 2019
Plasma acceleration

Motion in laser focus

- Single electron oscillating slightly off-centre of focused laser beam:



- After 1st quarter-cycle, sees **lower** field
 - Doesn't quite return to initial position
- ⇒ Accelerated away from axis

Courtesy of Paul Gibbon, CAS 2019

Ponderomotive force: transverse

In the limit $v/c \ll 1$, the equation of motion (25) for the electron becomes:

$$\frac{\partial v_y}{\partial t} = -\frac{e}{m} E_y(\mathbf{r}). \quad (21)$$

Taylor expanding electric field about the current electron position:

$$E_y(\mathbf{r}) \simeq E_0(y) \cos \phi + y \frac{\partial E_0(y)}{\partial y} \cos \phi + \dots,$$

where $\phi = \omega t - kx$ as before.

To lowest order, we therefore have

$$v_y^{(1)} = -v_{\text{os}} \sin \phi; \quad y^{(1)} = \frac{v_{\text{os}}}{\omega} \cos \phi,$$

where $v_{\text{os}} = eE_L/m\omega$.

Courtesy of Paul Gibbon, CAS 2019

Ponderomotive force: transverse (contd.)

Substituting back into Eq. (21) gives

$$\frac{\partial v_y^{(2)}}{\partial t} = -\frac{e^2}{m^2 \omega^2} E_0 \frac{\partial E_0(y)}{\partial y} \cos^2 \phi.$$

Multiplying by m and taking the laser cycle-average,

$$\bar{f} = \int_0^{2\pi} f \, d\phi,$$

yields the **transverse** ponderomotive force on the electron:

$$f_{py} \equiv m \overline{\frac{\partial v_y^{(2)}}{\partial t}} = -\frac{e^2}{4m\omega^2} \frac{\partial E_0^2}{\partial y}. \quad (22)$$

Courtesy of Paul Gibbon, CAS 2019

Ponderomotive force

Ponderomotive force

While the direct derivation of the relativistic ponderomotive force is quite involving, we can use identification of the ponderomotive potential as the mean kinetic energy of the quivering electrons as a short-cut:

$$\bar{E}_{kin} = \Phi_{pond} = -m_e c^2 \langle \gamma - 1 \rangle \stackrel{\gamma = \sqrt{1 + \frac{a_0^2}{2}}}{\propto} \sqrt{I}$$

This yields the relativistic ponderomotive force as:

$$\vec{F}_{pond} = -m_e c^2 \nabla \langle \gamma \rangle = -\frac{m_e c^2}{e} \nabla \sqrt{\frac{a_0^2}{2}}$$

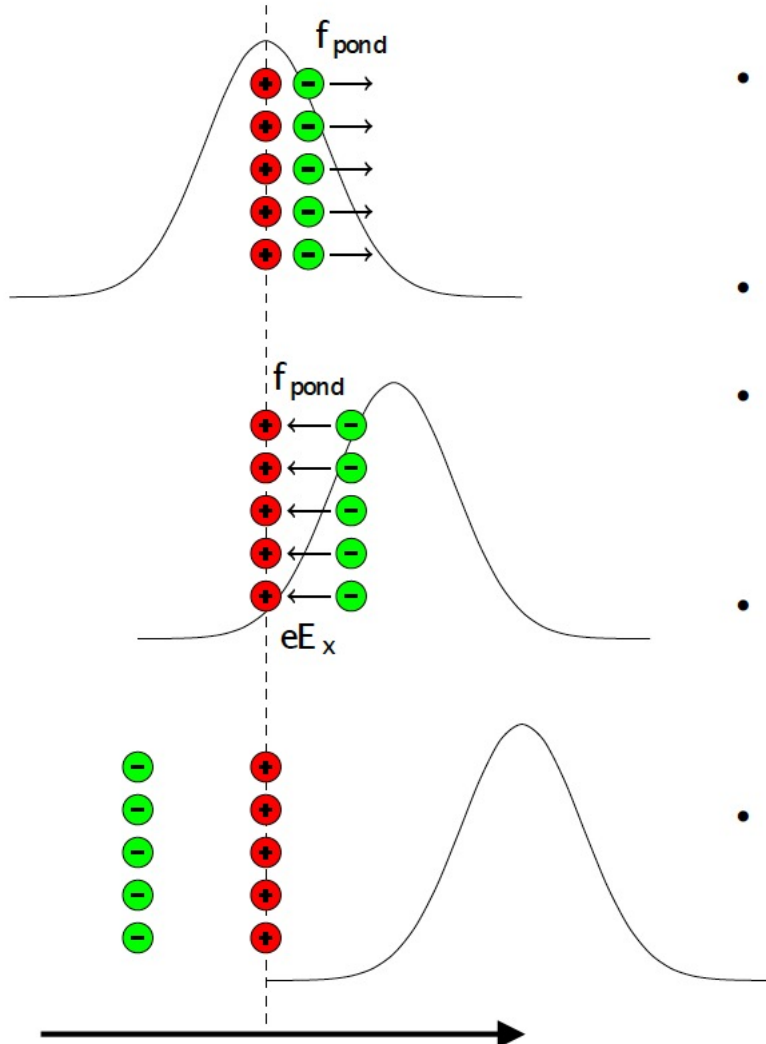
	non-relativistic	relativistic
F_{pond}	$-\frac{e^2}{4m_e \omega_L^2} \nabla(E_L^2)$	$-\frac{mc^2}{e} \nabla \sqrt{a_0^2/2}$
Φ_{pond}	$\frac{e^2}{4m_e \omega_L^2} E_L^2$	$\frac{mc^2}{e} \langle \gamma - 1 \rangle$
proportionality	$I, \nabla I$	$\sqrt{I}, \nabla \sqrt{I}$

Courtesy of Stephan Karsch, CAS 2019

Plasma acceleration

Ponderomotive force

Double ponderomotive push

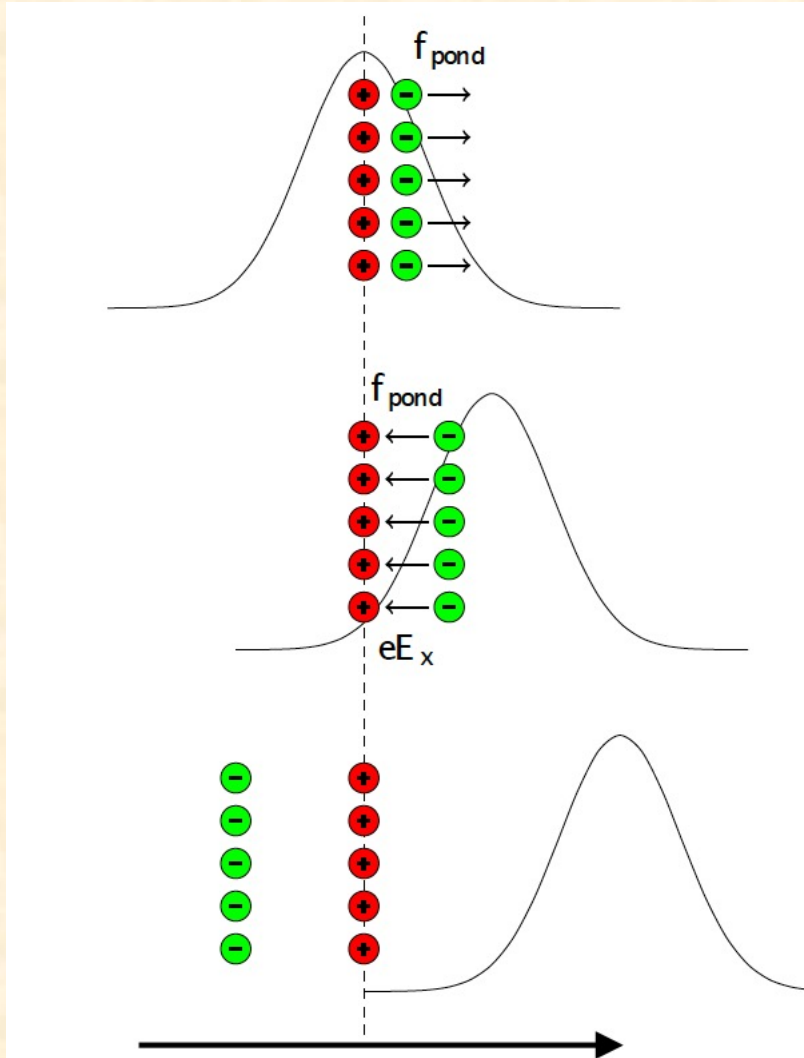


- Two kicks by the ponderomotive force, corresponding to the rising and the falling edge of the laser pulse.
- Optimum pulse duration $\tau_{FWHM} = 0.37 \lambda_p / c$.
- Wake excitation is dominated by the rising edge kick due to longer interaction between co-moving electrons and driver.
- Resulting charge separation separation causes electric fields to exhibit a strong longitudinal component.
- The wave structure travels with $v_{ph} = c\eta$, and hence can constantly accelerate a co-moving electron.

Courtesy of Stephan Karsch, CAS 2019
Plasma acceleration

Quizz:

Increasing the pressure

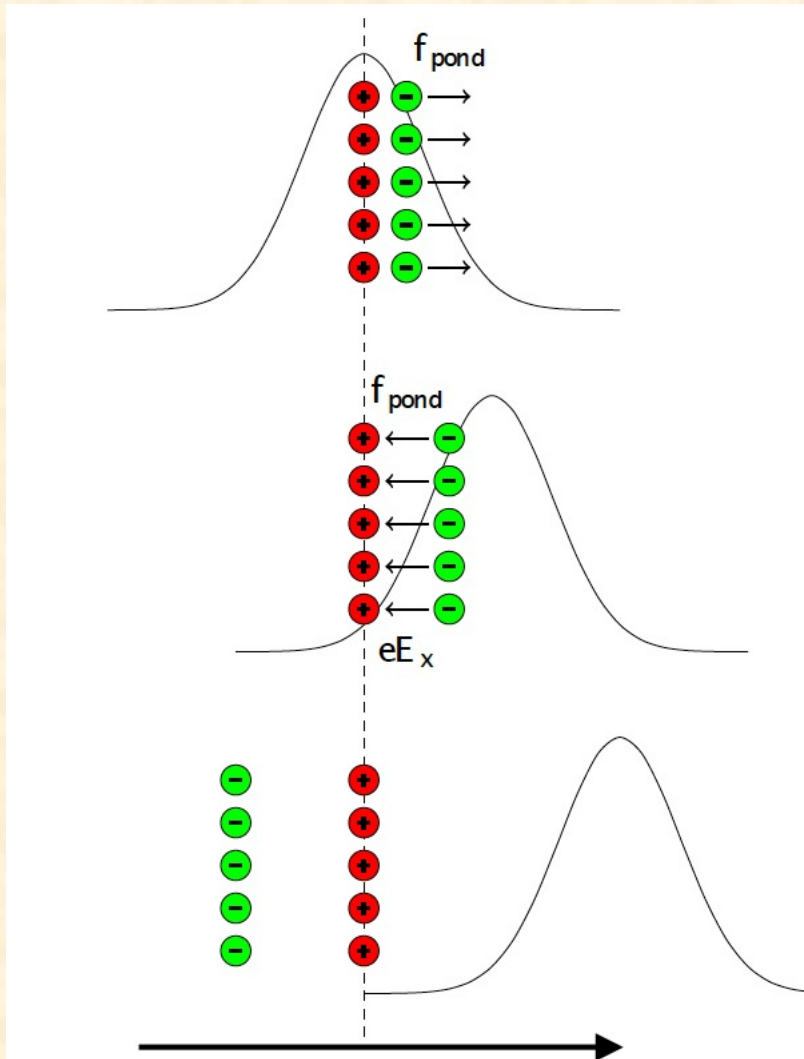


What happens if the gas pressure is increased?

- (a) Nothing
- (b) The number of electrons creating the field will be higher and hence there will be a higher accelerating gradient
- (c) Proportionally fewer electrons will be displaced and hence the gradient will be lower.

Quizz:

Answer (b)



The number of electrons creating the field will be higher and hence there will be a higher accelerating gradient

Linear wakefield

Linear wakefields

For small laser intensities ($a_0 \ll 1$), the plasma density is only weakly perturbed $\delta n_e \ll n_{e,0}$ and the continuity equation can be written as:

$$\frac{\partial \delta n_e}{\partial t} + n_{e,0} \nabla \vec{v} = 0$$

The above expression and Poisson's equation can be now inserted into the derivative of the Lorentz force. Keeping in mind $\nabla A = 0$ (Coulomb gauge) and $\mathbf{p} = m_e \mathbf{v}$ yields for initially resting electrons at low intensities, i.e., $\gamma = 1 + a^2/2$:

$$\left(\frac{\partial^2}{\partial t^2} + \omega_p^2 \right) \frac{\delta n_e}{n_{e,0}} = c^2 \nabla^2 \frac{a^2}{2}$$

The RHS represents the driving term of a forced oscillator, and is proportional to the ponderomotive force $F_{\text{pond}} = m_e c^2 \nabla^2 a^2 / 2$. With Poisson's equation we express the charge imbalance with the scalar wake potential in the moving frame coordinates ($\xi = z - v_g t$, $\tau = t$)

$$\left(\frac{\partial^2}{\partial \xi^2} + k_p^2 \right) \phi = k_p^2 \frac{a^2}{2}$$

Assuming a radial symmetry, an analytical solution of the inhomogeneous wave equation can be found in 3D. It is given by

$$\phi(r, \xi) = -\frac{k_p}{4} \int_{\xi}^{\infty} a^2(r, \xi') \sin(k_p (\xi - \xi')) d\xi'$$

Courtesy of Stephan Karsch, CAS 2019

Plasma acceleration

Linear wakefield

Linear wakefields II

For a Gaussian laser envelope $a = a_0 \exp(-\xi^2/(c\tau_0)^2) \exp(-r^2/w_0^2)$, the solution of the integral for $\xi \rightarrow -\infty$, i.e. after the laser transit is given by:

$$\phi(r, \xi) = -a_0^2 \sqrt{\frac{\pi}{2}} \frac{k_p}{4} c\tau_0 e^{-(2r^2/w_0^2)} e^{-(k_p c\tau_0)^2/8} \sin(k_p \xi)$$

From this scalar potential ϕ the electric field and the electron density can be derived as:

$$\frac{E_z}{E_{p,0}} = -\frac{1}{k_p} \frac{\partial \phi}{\partial \xi}, \quad \frac{E_r}{E_{p,0}} = -\frac{1}{k_p} \frac{\partial \phi}{\partial r}, \quad \frac{\delta n_e}{n_{e,0}} = -\frac{1}{k_p^2} \frac{\partial^2 \phi}{\partial \xi^2},$$

$E_{p,0}$ corresponds to the maximal electric field of the plasma wave in the linear regime, known as the cold fluid wavebreaking field:

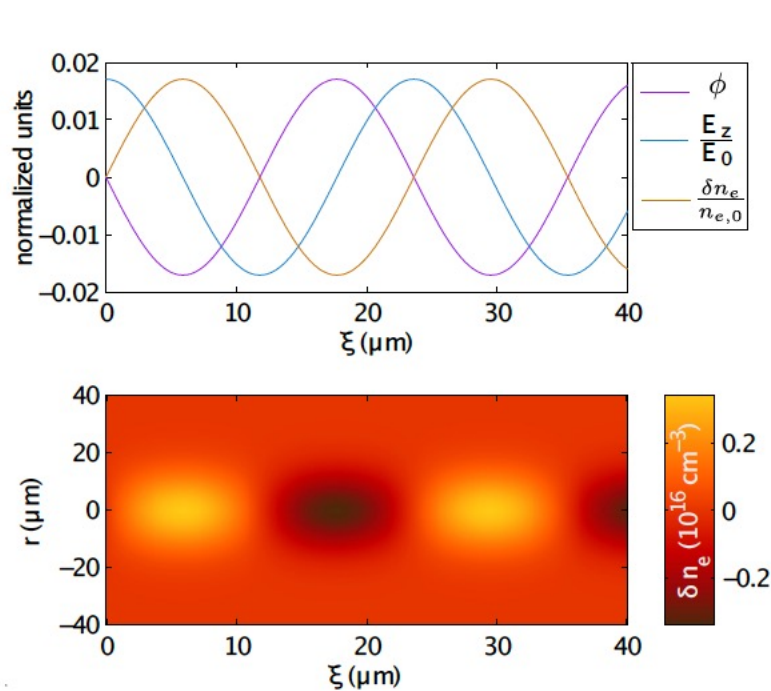
$$E_{p,0} = \frac{m_e c \omega_p}{e}, \quad E_{p,0} [\text{GV/m}] = 96 \sqrt{n_{e,0} [10^{18} \text{cm}^{-3}]}$$

Courtesy of Stephan Karsch, CAS 2019

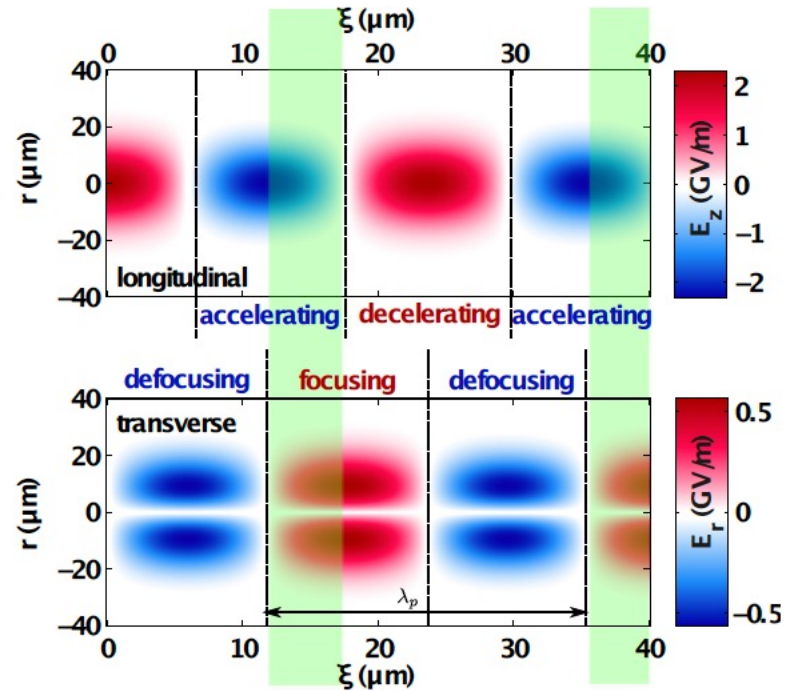
Plasma acceleration

Linear wakefield

Linear wakefields III



Top: Normalized plasma potential ϕ , longitudinal electric field E_z/E_0 and density perturbation $\delta n_e/n_{e,0}$ on axis ($r = 0$). Bottom: color coded plasma density perturbation $\delta n_e(r, \xi)/n_{e,0}$ generated by the ponderomotive force in the vicinity of a Gaussian laser focus.



top: Spatial extent of the longitudinal $E_z(r, \xi)$ and bottom: the radial electric field $E_r(r, \xi)$. The green area marks a $\lambda_p/4$ -phase region of the wakefield with an accelerating and transverse focusing field.

3D linear wakefield quantities in the co-moving frame created by a laser pulse with $a_0 = 0.2$, $t_{\text{FWHM}} = 28 \text{ fs}$ and $d_{\text{FWHM}} = 22 \mu\text{m}$ in a plasma density of $2 \times 10^{18} \text{ cm}^{-3}$

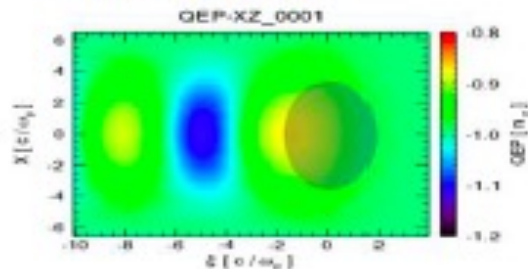
Courtesy of Stephan Karsch, CAS 2019

Plasma acceleration

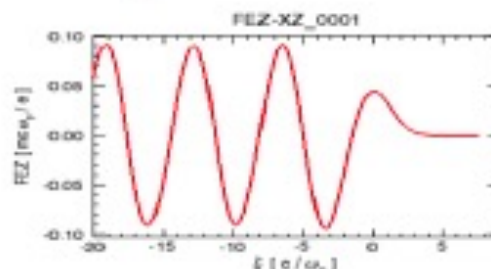
From linear to non-linear

From Linear to Non-Linear

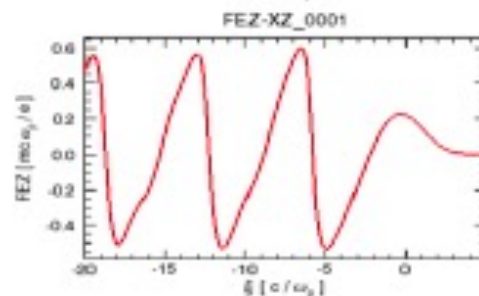
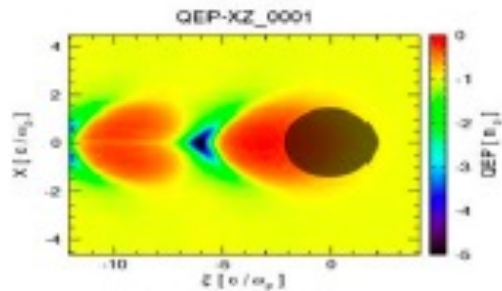
Electron density :



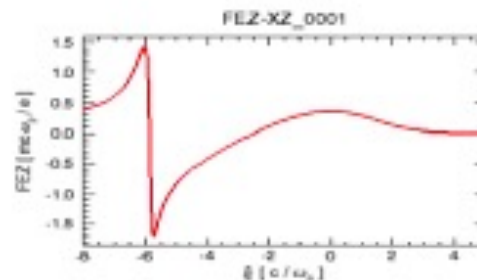
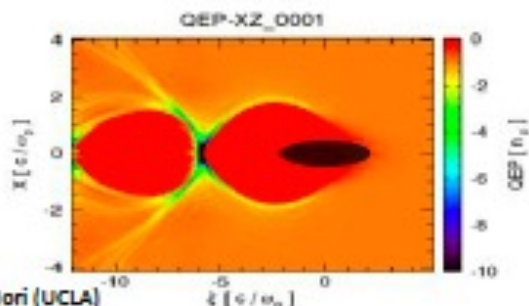
Longitudinal fields :



$n_b \ll n_{pe}$ – linear regime



$n_b \sim n_{pe}$ – non-linear wakes



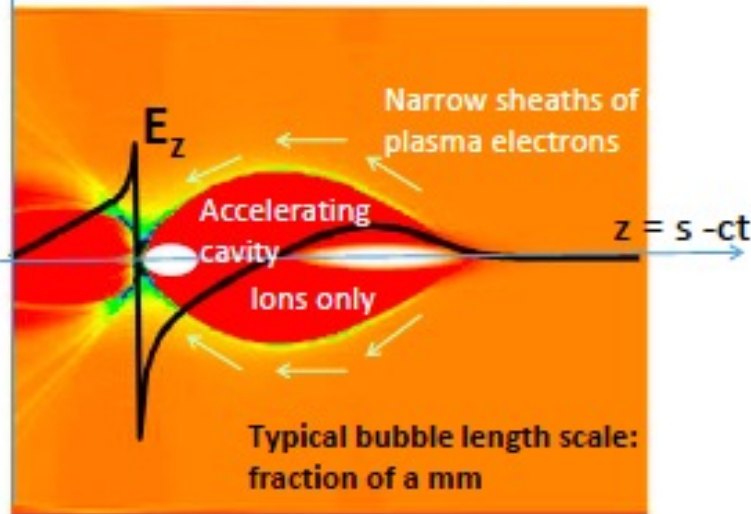
$n_b \gg n_{pe}$ – blow-out regime

W. Mori (UCLA)

Courtesy of Edda Gschwendtner, CAS 2019
Plasma acceleration

Blow-out regime

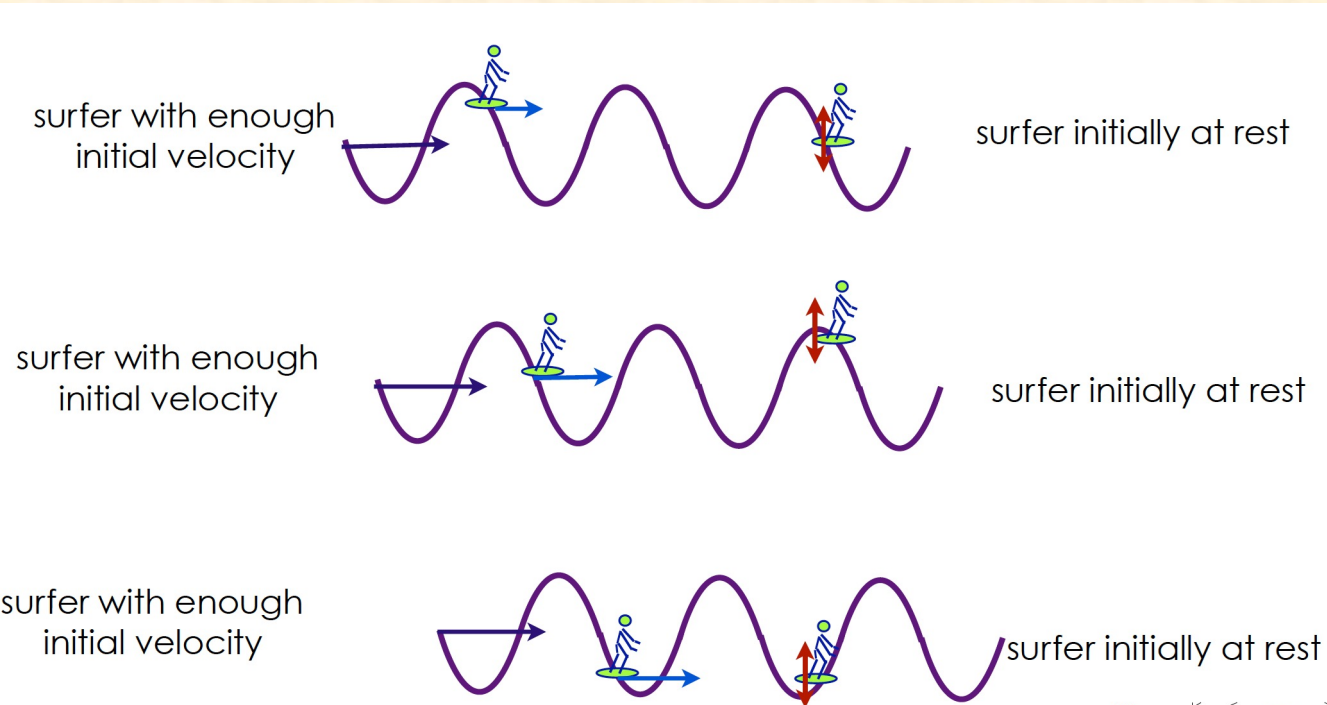
Blow-out Regime



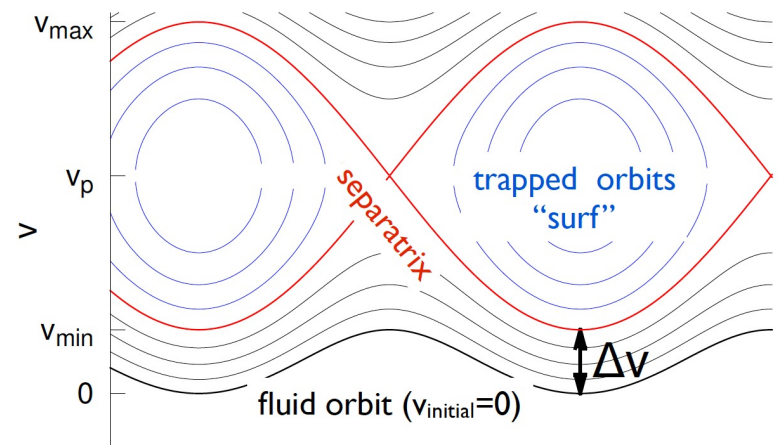
- Space-charge force of the driver blows away all the plasma electrons in its path, leaving a uniform layer of ions behind (ions move on a slower time scale).
- Plasma electrons form a narrow sheath around the evacuated area, and are pulled back by the ion-channel after the drive beam has passed
- An accelerating cavity is formed in the plasma
- The back of the blown-out region: ideal for electron acceleration

- High charge witness acceleration possible → charge ratio to witness of same order
- Linear focusing in r , for electrons; very strong quadrupole (MT/m)
- High transformer ratios (>2) can be achieved by shaping the drive bunch
- E_r independent of x , can preserve incoming emittance of witness beam

Surfing the wave



Courtesy of V. Malka



Trapping condition

Trapping condition

When can an electron be trapped in the plasma wave?

Consider Hamiltonian of an electron interacting with the laser field in the presence of a plasma wave (normalized quantities):

$$H(z, u_z) = \underbrace{\sqrt{1 + u_{\perp}^2 + u_z^2}}_{=\gamma} - \phi(z - v_g t)$$

For an initially resting electron, due to conservation of canonical momentum, $u_{\perp} = a$. The second term represents the wave's potential. The time dependence can be eliminated by a canonical transformation $(z, u_z) \rightarrow (\xi, u_z)$ ¹. The time-independent Hamiltonian then reads:

$$H(z, u_z) = \sqrt{1 + a(\xi)^2 + u_z(\xi)^2} + \phi(\xi) - \beta_g u_z(\xi)$$

$H(\xi, u_z) = H_0 = \text{const.}$ describes the motion of an electron with an initial energy $E = H_0$ on a distinct orbit in the plasma wave. Solving the expression for the Hamiltonian for $u_z(\xi)$ gives the trajectory of the electron in the longitudinal phase space (ξ, u_z) :

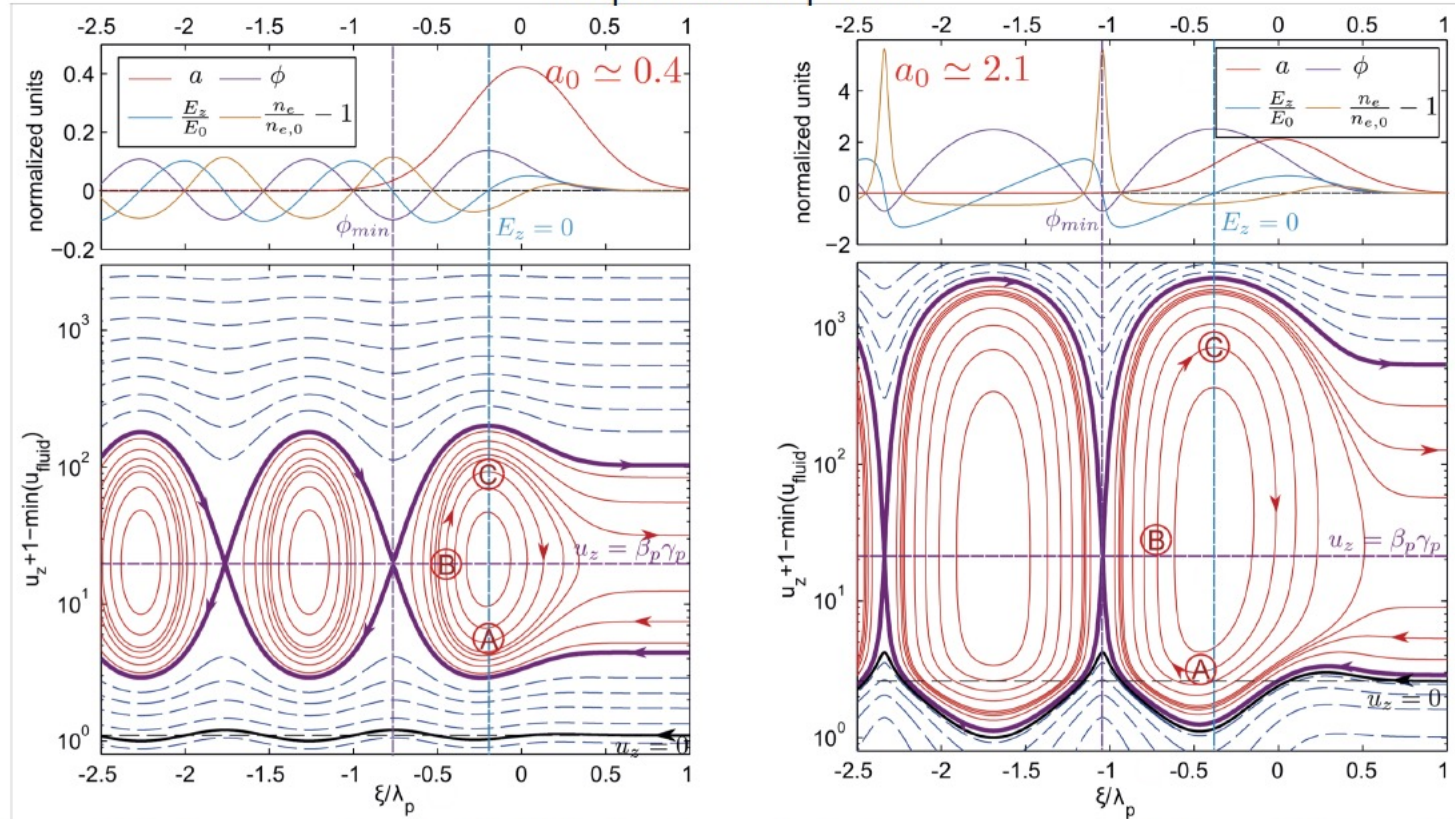
$$u_z = \beta_g \gamma_g^2 (H_0 + \phi) \pm \gamma_g \sqrt{\gamma_g^2 (H_0 + \phi)^2 - \gamma_{\perp}^2}$$

$u_z(\xi)$ represents an electron orbit of constant total energy for a given set of $a(\xi)$, $\phi(\xi)$ and H_0

¹With a generating function $F(z, u_z) = u_z \times (z - v_g t)$ the new Hamiltonian reads $H = H' - 1/c \frac{\partial F}{\partial t}$

Trapping condition

Separatrix plots

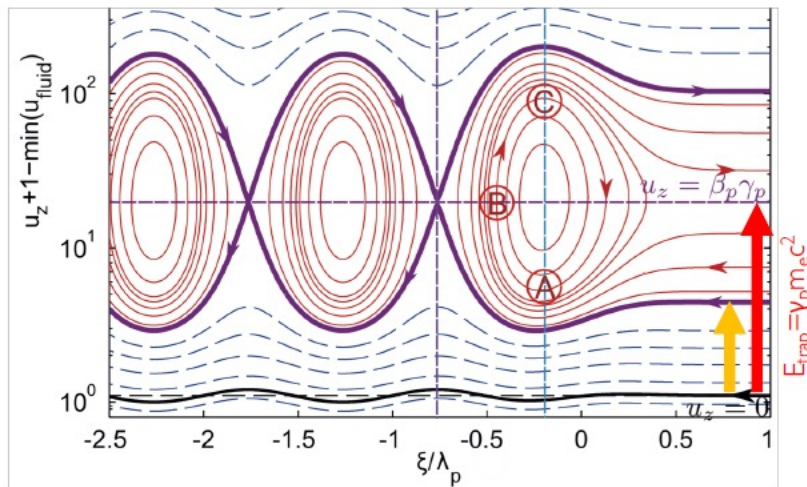


(red): trapped electrons on closed orbit. (blue): untrapped electrons on open orbit. (purple) Separatrix separating open and closed orbits with a radicand equal to zero. It crosses itself at $\phi = \min$ (purple vertical line). The Hamiltonian of the separatrix is given by $H_{\text{sep}} = v_{\perp}(\xi_{\min})/v_g - \phi_{\min}$. Electrons initially at rest ($H_{\text{fluid}} = 1, u_{\perp}(\xi = +\infty) = u_z(\xi = +\infty) = 0$, black) do not gain momentum from the plasma wave. Electrons with a too low/high initial momentum (dashed blue lines) $|H_0| > |H_{\text{sep}}|$ are moving on open orbits

Courtesy of Stefan Karsch, CAS 2019

Trapping condition

Trapping condition for e^- overtaken by wakefield (external injection)



In 1-D, the trapping condition reads:

$$E_{trap} = m_e c^2 \left(\sqrt{1 + u_{z,sep}^2(+\infty)} - 1 \right)$$

with:

$$u_{z,sep}(+\infty) = \beta_p \gamma_p^2 H_{sep} - \gamma_p \sqrt{\gamma_p^2 H_{sep}^2 - 1}$$

being the separatrix distance in front of the laser ($a_0 = \phi = u_\perp = 0$)

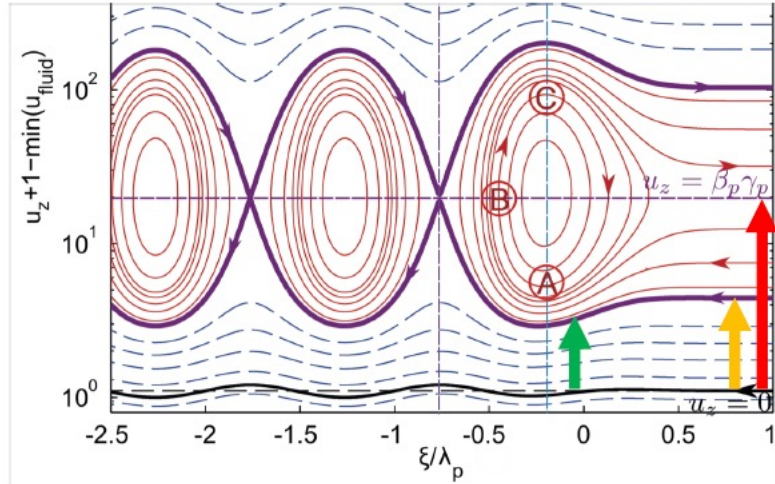
- Electrons with a forward momentum substantially lower (how much depends on wake amplitude) can be caught and gain maximum energy at point C if acceleration would terminate there.

Courtesy of Stefan Karsch, CAS 2019

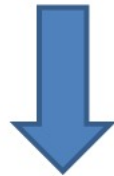
Plasma acceleration

Trapping condition

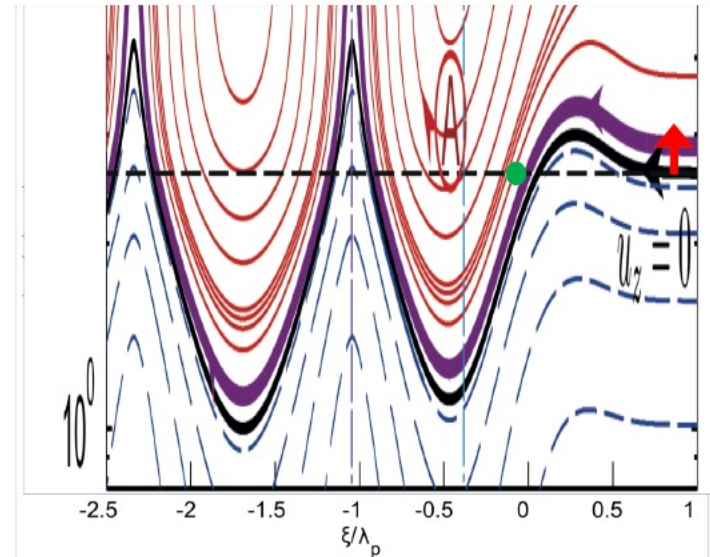
How about even lower thresholds?



Electrons gain threshold energy inside wake bucket



Colliding pulse injection



Electrons are born inside wake bucket



Ionization injection

Courtesy of Stefan Karsch, CAS 2019
Plasma acceleration

Trapping condition

Colliding pulse (beat wave) injection

Consider two counter-propagating, c.p. laser pulses:

$$a_{1/2} = \frac{a_{1/2}(t)}{\sqrt{2}} \left(\cos(k_L z \pm \omega_L t) \vec{e}_x + \sin(k_L z \pm \omega_L t) \vec{e}_y \right)$$

where $a_{0,1/2}(t)$ are the temporal pulse shapes for both pulses

With the beat-wave Hamiltonian

$$H_{beat} = \sqrt{1 + u_{\perp}^2 + u_z^2} = \sqrt{1 + (a_1 + a_2)^2 + u_z^2}$$

we get a beat-wave separatrix:

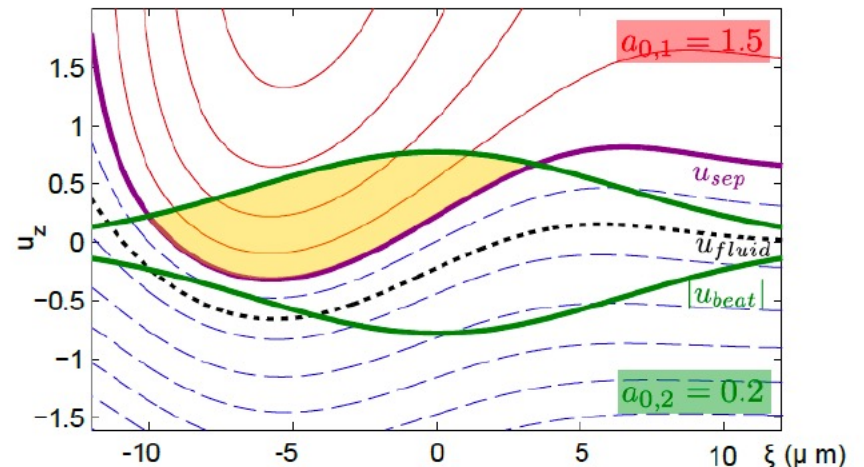
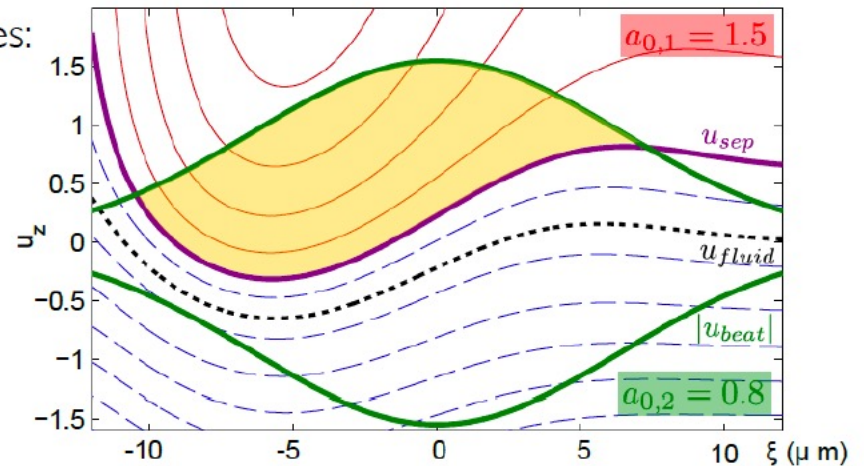
$$u_{beat}(t) = \pm \sqrt{a_{0,1}(t) a_{0,2}(t) (1 - \cos(2\omega_L t))}$$

$$u_{beat,max/min}(t) = \pm \sqrt{2a_{0,1}(t) a_{0,2}(t)}$$

$$W_{beat}(t) = m_e c^2 \sqrt{1 + u_{beat}(t)^2} - 1$$

Injection if (in co-moving frame):

$$u_{beat,max}(\xi) > u_{sep}(\xi)$$



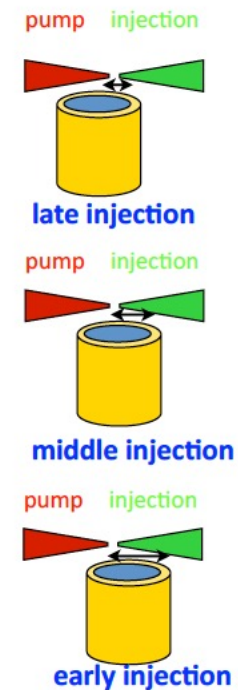
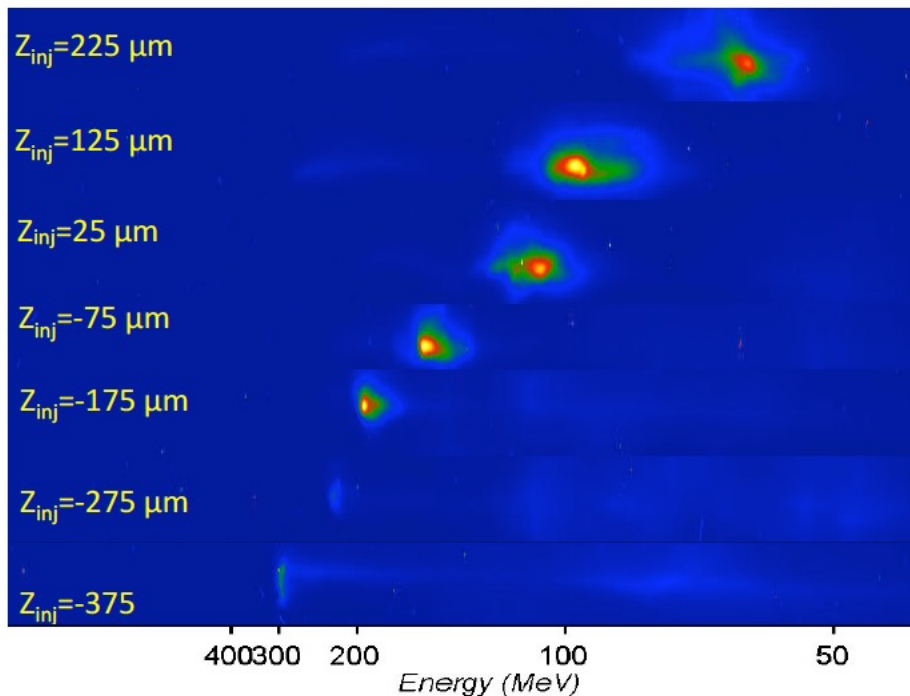
Courtesy of Stefan Karsch, CAS 2019

Plasma acceleration

Trapping condition

Colliding pulse (beat wave) injection exp.

- Localized injection leading to quasi-monochromatic beams
- Adjustable energy via tuning of collision (injection) position



J Faure et al., Nature 444, 737 (2006)

Courtesy of Stejan Karsch, CAS 2019
Plasma acceleration

Trapping condition

Ionization injection

Gas target contains traces of high- Z gas, which is ionized by the peak of the laser and born at $\xi_{\text{ion}} \sim 0$ at rest ($u_z(\xi_{\text{ion}}) \sim 0$):

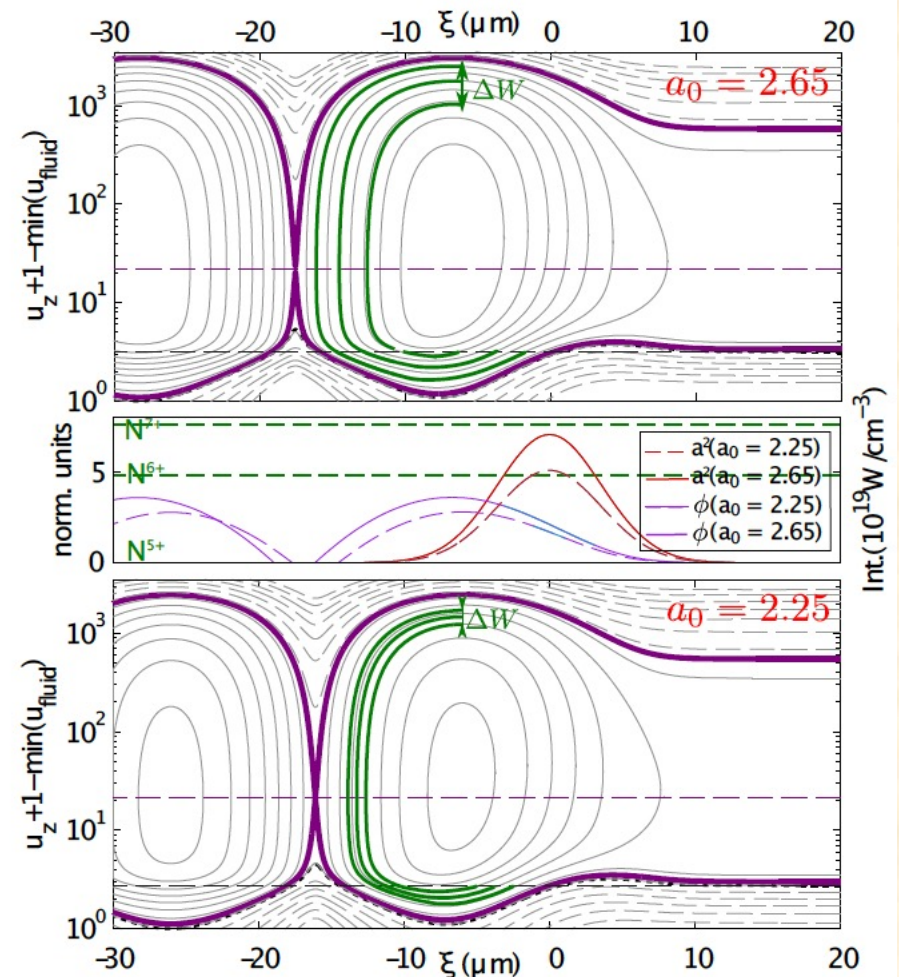
$$H_{\text{ion}} = 1 - \phi(\xi_{\text{ion}})$$

Trapping condition¹ for sin-envelope pulses:

$$1 - \gamma_p^{-1} \leq \phi(\xi_{\text{ion}}) - \phi_{\text{min}} \leq \phi_{\text{max}} - \phi_{\text{min}} \sim \underbrace{\left(\frac{\pi}{8} + \frac{1}{4} \right)}_{\sim 0.64} a_0^2$$

Ionization injection only works for relativistic intensity ($a_0^2 > 1.6$) pulses!

(even if ionization threshold would be lower)

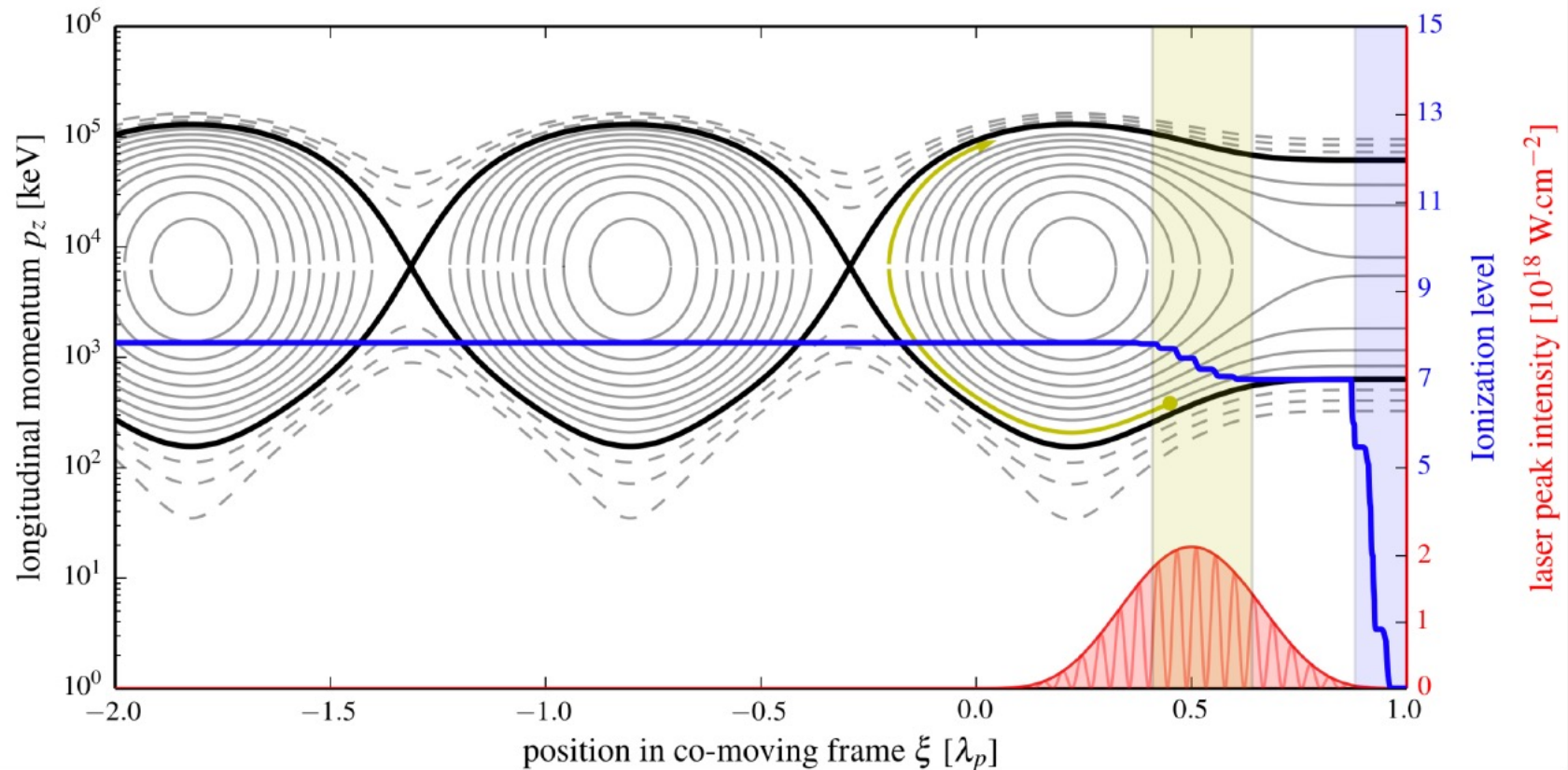


¹Chen et al, Phys. Plasmas 19, 033101 (2012)

Trapping condition

Ionization injection II

Oxygen trace gas

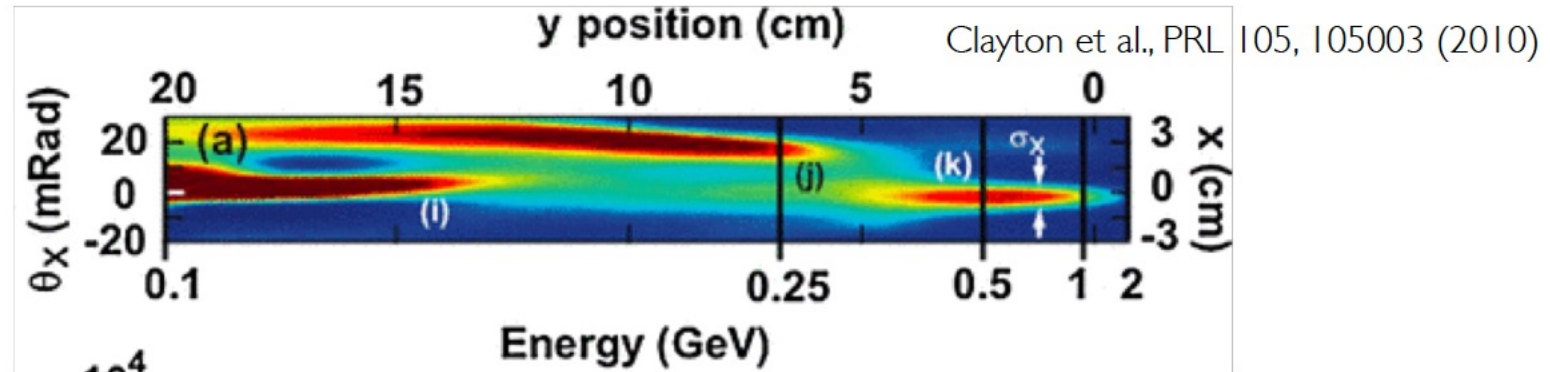


Courtesy of Stefan Karsch, CAS 2019
Plasma acceleration

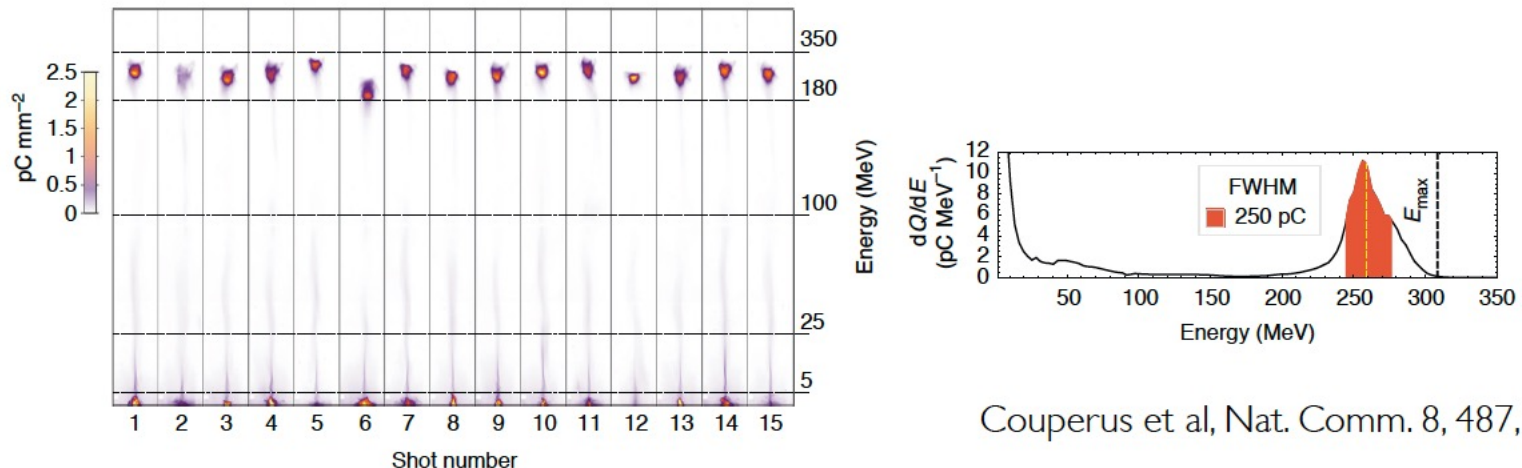
Trapping condition

Ionization injection exp.

- Constant injection commonly leads to broadband spectra, but high charge...



- ... which can be used to fully beamload and truncate the injection



Couperus et al, Nat. Comm. 8, 487, 2017

Courtesy of Stefan Karsch, CAS 2019
Plasma acceleration

Trapping condition

„Longitudinal injection“

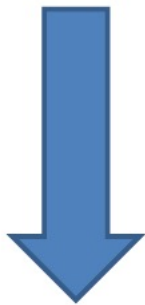
Instead of giving an electron the correct energy at the correct phase, it is possible to shift the wake phase to gobble up electrons from other phase positions.

Any sudden shift in plasma wavelength our driving phase will shift the wake phase.

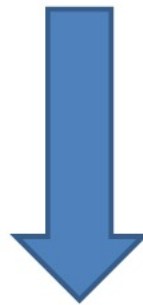
Shift by laser intensity variation

Shift by density step / slope

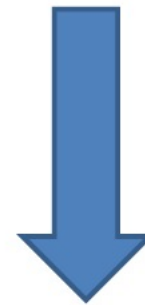
Shift by driver swap



longitudinal/transverse
self-injection



density
down ramp/shock front
injection



Hybrid
injection

all these schemes will cause the wave to break momentarily or continuously

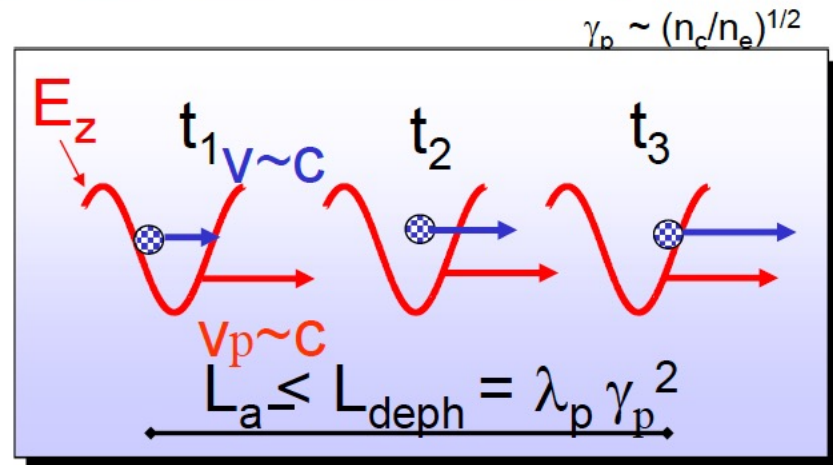
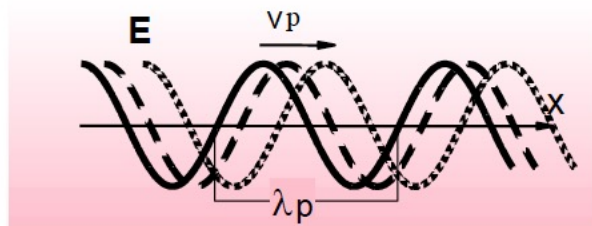
Courtesy of Stefan Karsch, CAS 2019

Plasma acceleration

Dephasing length

Relativistic electrons are trapped and accelerated over the dephasing length

- ➡ Relativistic plasma wave:
Too slow or too fast electrons do not stay long with the wave



B. Cros, CAS HGWA Sesimbra, March 2019

Courtesy of Brigitte Cros, CAS 2019
Plasma acceleration

Dephasing length

Energy gain over dephasing length



➡ Energy gain

$$\Delta W = e E_z L_a \sim 4mc^2 \gamma_p^2$$

➡ Relativistic factor

$$\gamma_p \sim (n_c/n_e)^{1/2}$$

$$\gamma_p = \lambda_p / \lambda_0$$

$$L_a < L_{\text{deph}} = \lambda_p \gamma_p^2$$



n_e	10^{17}cm^{-3}	10^{19}cm^{-3}
γ_p	100	10
L_a	1 m	1 mm
ΔW_{max}	20 GeV	200 MeV

B. Cros, CAS HGWA Sesimbra, March 2019

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Courtesy of Brigitte Cros, CAS 2019
Plasma acceleration

Some simple equations

Some simple equations about laser-plasma acceleration

- Plasma:

$$n_e [cm^{-3}] = 2,429 \times 10^{16} \times Z \times p [mbar]$$

$$n_e [10^{17} cm^{-3}] = 0,486 p [mbar]. \quad \text{For H}_2 \text{ or He}$$

$$\omega_p = \sqrt{\frac{n_e e^2}{m \epsilon_0}}$$

Plasma pulsation

$$\frac{\omega}{\omega_p} = \sqrt{\frac{n_c}{n_e}}$$

$$n_c = \frac{1,11485 \times 10^{21}}{\lambda^2 [\mu m^2]} cm^{-3}$$

Critical density.
Typically $n_e \ll n_c$ in ALP

$$\lambda_p = \lambda \times \sqrt{\frac{n_c}{n_e}}$$

Some simple equations about laser-plasma acceleration

- Laser:

$$a_0 = 0,855 \sqrt{I \left[10^{18} W / cm^2 \right] \times \lambda^2 \left[\mu m^2 \right]}$$

- Acceleration:

$$E_0 = \frac{mc\omega_p}{e} = \frac{2\pi mc^2}{e} \times \frac{1}{\lambda_p}$$

$$E_0 \left[GV / m \right] = \frac{3,2107 \times 10^{12}}{\lambda_p \left[\mu m \right]}$$

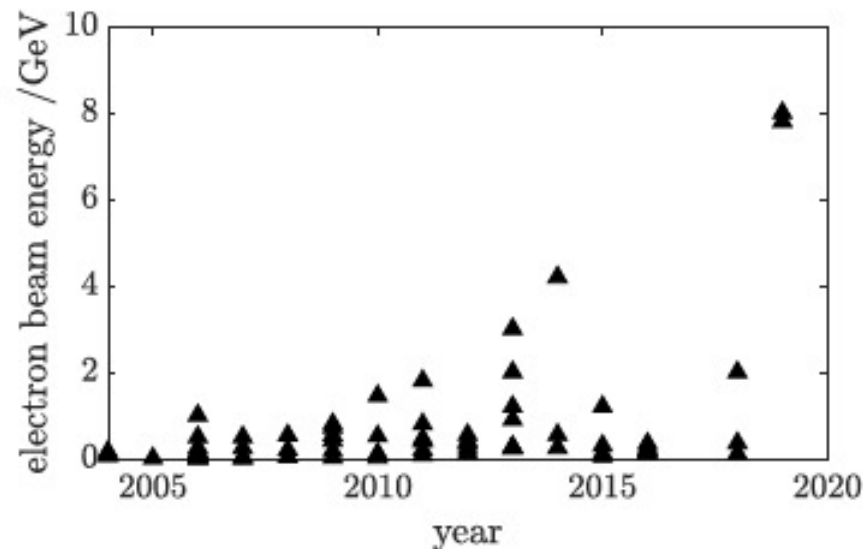
$$E_0 \left[GV / m \right] = 96,159 \sqrt{n_e \left[10^{18} cm^{-3} \right]}$$

The higher the gas pressure the better gradient but the shorter the plasma wavelength (ie the trapping volume)

Some experimental results

Some experimental results

Fast progress in electron beam energy



- Electron beam from laser wakefield accelerators has been going up steadily since 2004 results.

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

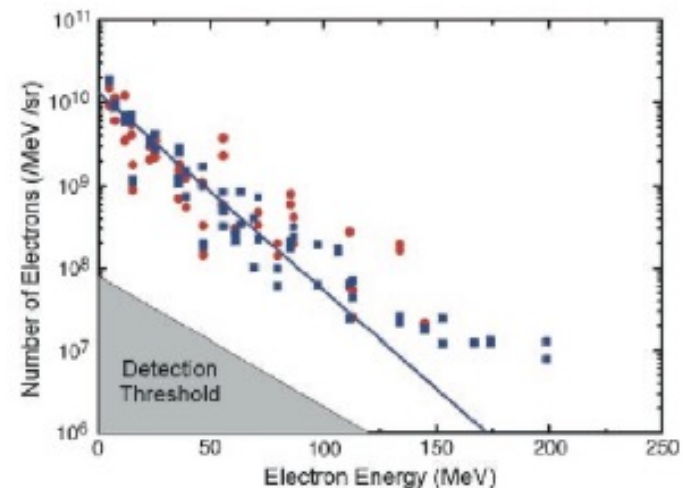
Some experimental results

Experiments at the energy frontier: 2002

Electron Acceleration by a Wake Field Forced by an Intense Ultrashort Laser Pulse

V. Malka,^{1*} S. Fritzler,¹ E. Lefebvre,² M.-M. Aleonard,³ F. Burgy,¹ J.-P. Chambaret,¹ J.-F. Chemin,³ K. Krushelnick,⁴ G. Malka,³ S. P. D. Mangles,⁴ Z. Najmudin,⁴ M. Pittman,¹ J.-P. Rousseau,¹ J.-N. Scheurer,³ B. Walton,⁴ A. E. Dangor⁴

Plasmas are an attractive medium for the next generation of particle accelerators because they can support electric fields greater than several hundred gigavolts per meter. These accelerating fields are generated by relativistic plasma waves—space-charge oscillations—that can be excited when a high-intensity laser propagates through a plasma. Large currents of background electrons can then be trapped and subsequently accelerated by these relativistic waves. In the forced laser wake field regime, where the laser pulse length is of the order of the plasma wavelength, we show that a gain in maximum electron energy of up to 200 megaelectronvolts can be achieved, along with an improvement in the quality of the ultrashort electron beam.



V. Malka, *Science*, 298, 1596-1600 (2002)

- Extends to 200 MeV
- $n_e = 2.5 \times 10^{19} \text{ cm}^{-3}$, 3 mm gas jet
- $P = 33 \text{ TW}$, "Salle Jaune" laser at LOA

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

Some experimental results

Experiments at the energy frontier: 2006

GeV electron beams from a centimetre-scale accelerator

W. P. LEEMANS^{1,*}, B. NÄGLER¹, A. J. GONSALVES², Cs. TÓTH¹, K. NAKAMURA^{1,3}, C. G. R. GEDDES¹, E. ESAREY^{1*}, C. B. SCHROEDER¹ AND S. M. HOOKER²

¹Lawrence Berkeley National Laboratory, 1 Cyclotron Road, Berkeley, California 94720, USA

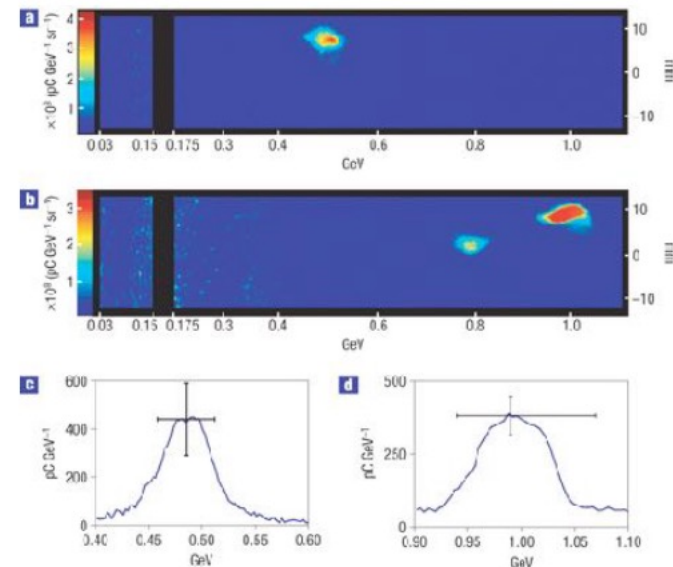
²University of Oxford, Clarendon Laboratory, Parks Road, Oxford OX1 3PU, UK

³Nuclear Professional School, University of Tokyo, 22-2 Shirane-shinkai, Tokyo, Naka, Ibaraki 319-1188, Japan

*Also at: Physics Department, University of Nevada, Reno, Nevada 89567, USA

*e-mail: W.P.leemans@lbl.gov

W.P. Leemans, Nature Physics, 2, 696-699 (2006)



- 1.0 GeV
- $n_e = 4.3 \times 10^{18} \text{ cm}^{-3}$, 33 mm capillary discharge waveguide
- $P = 40 \text{ TW}$, TREX laser at LBNL

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

Some experimental results

Experiments at the energy frontier: 2010

Self-Guided Laser Wakefield Acceleration beyond 1 GeV Using Ionization-Induced Injection

C. E. Clayton,^{1,*} J. E. Ralph,² F. Albert,² R. A. Fonseca,³ S. H. Glenzer,² C. Joshi,¹ W. Lu,¹ K. A. Marsh,¹ S. F. Martins,² W. B. Mori,¹ A. Pak,¹ F. S. Tsung,¹ B. B. Pollock,^{2,4} J. S. Ross,^{2,4} L. O. Silva,² and D. H. Froula²

¹Department of Electrical Engineering, University of California, Los Angeles, California 90095, USA

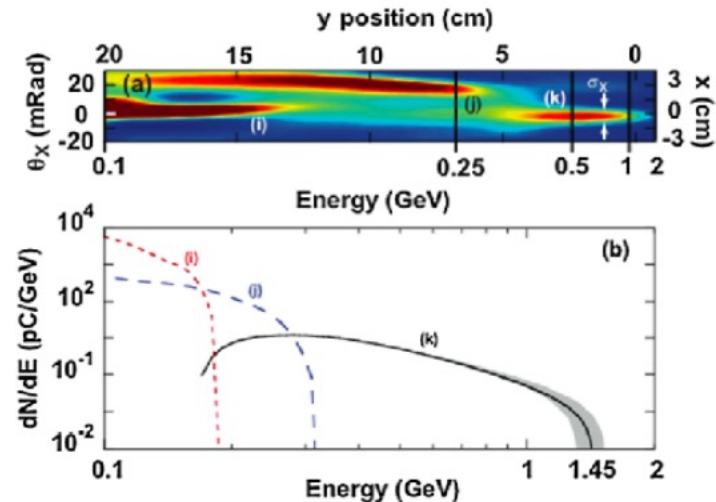
²L-399, Lawrence Livermore National Laboratory, P.O. Box 808, Livermore, California 94551, USA

³God. P11P7N-LA, Instituto Superior Técnico, Lisboa, Portugal

⁴MAE Department, University of California, San Diego, La Jolla, California 92093, USA
(Received 23 April 2010; published 1 September 2010)

The concepts of matched-beam, self-guided laser propagation and ionization-induced injection have been combined to accelerate electrons up to 1.45 GeV energy in a laser wakefield accelerator. From the spatial and spectral content of the laser light exiting the plasma, we infer that the 60 fs, 110 TW laser pulse is guided and excites a wake over the entire 1.3 cm length of the gas cell at densities below $1.5 \times 10^{18} \text{ cm}^{-3}$. High-energy electrons are observed only when small (3%) amounts of CO_2 gas are added to the He gas. Computer simulations confirm that it is the K -shell electrons of oxygen that are ionized and injected into the wake and accelerated to beyond 1 GeV energy.

C. Clayton, Phys. Rev. Lett, 105, 105003 (2010)



- Extends to 1.45 GeV
- $n_e = 4.3 \times 10^{18} \text{ cm}^{-3}$, 1.3 cm gas cell
- P = 220 TW Callisto Laser at LLNL

Courtesy of Stuart Mangles, CAS 2019

Plasma acceleration

Some experimental results

Experiments at the energy frontier: 2013

ARTICLE

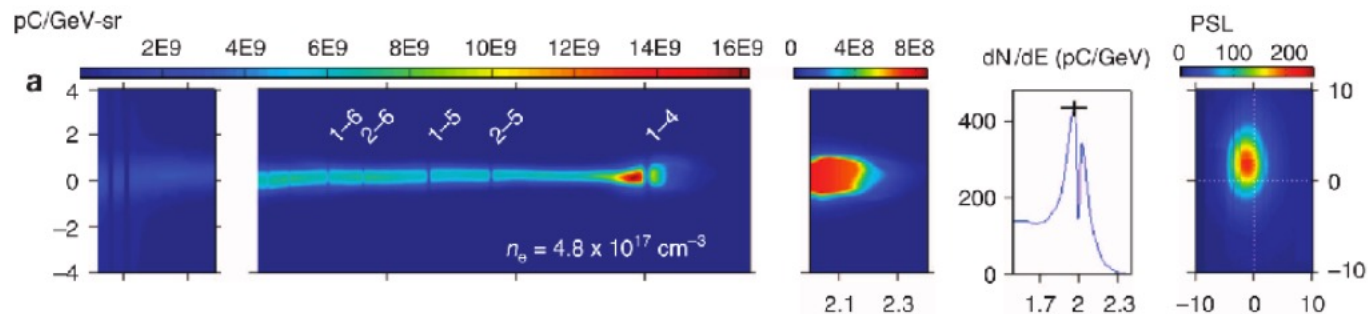
Received 2 Dec 2012 | Accepted 8 May 2013 | Published 11 Jun 2013

DOI: 10.1038/ncomms2988

OPEN

Quasi-monoenergetic laser-plasma acceleration of electrons to 2 GeV

Xiaoming Wang¹, Refal Zgadzaj¹, Neil Fazel¹, Zhengyan Li¹, S. A. Yi¹, Xi Zhang¹, Watson Henderson¹, Y.-Y. Chang¹, R. Korzekwa¹, H.-E. Tsai¹, C.-H. Pai¹, H. Quevedo¹, G. Dyer¹, E. Gaul¹, M. Martinez¹, A. C. Bernstein¹, T. Borger¹, M. Spinks¹, M. Donovan¹, V. Khudik¹, G. Shvets¹, T. Ditmire¹ & M. C. Downer¹



X. Wang, Nature Communications, 4, 1988 (2013)

- 2 GeV
- $n_e = 4.8 \times 10^{17} \text{ cm}^{-3}$, 7 cm gas cell
- $P = 1000 \text{ TW}$ “Texas PetaWatt” at University of Texas

Courtesy of Stuart Mangles, CAS 2019

Plasma acceleration

Some experimental results

Experiments at the energy frontier: 2014

Accepted Paper

Multi-GeV electron beams from capillary-discharge-guided subpetawatt laser pulses in the self-trapping regime

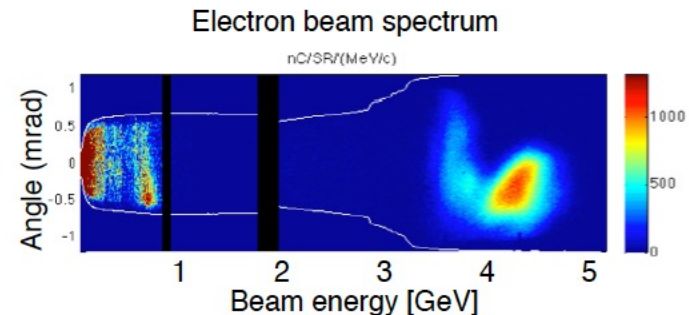
Phys. Rev. Lett.

W. P. Leemans, A. J. Gonsalves, H. S. Mao, K. Nakamura, C. Benedetti, C. B. Schroeder, Cs. Tóth, J. Daniels, D. E. Mittelberger, S. S. Bulanov, J.-L. Vay, C. G. R. Geddes, and E. Esarey

Accepted 21 October 2014

ABSTRACT

Multi-GeV electron beams with energy up to 4.2-GeV, 6-1% rms energy spread, 61 pC total charge, and 0.3% (milliradian) rms divergence have been produced from a 8.5-cm-long capillary discharge waveguide with a plasma density of approx $7 \times 10^{17} \text{ cm}^{-3}$, powered by laser pulses with peak power up to 0.3-PW. Preformed plasma waveguides allow the use of lower laser power compared to unguided plasma structures to achieve the same electron beam energy. Detailed comparison between experiment and simulation indicates the sensitivity in this regime of the guiding and acceleration in the plasma structure to input intensity, density, and near-field laser mode profile.

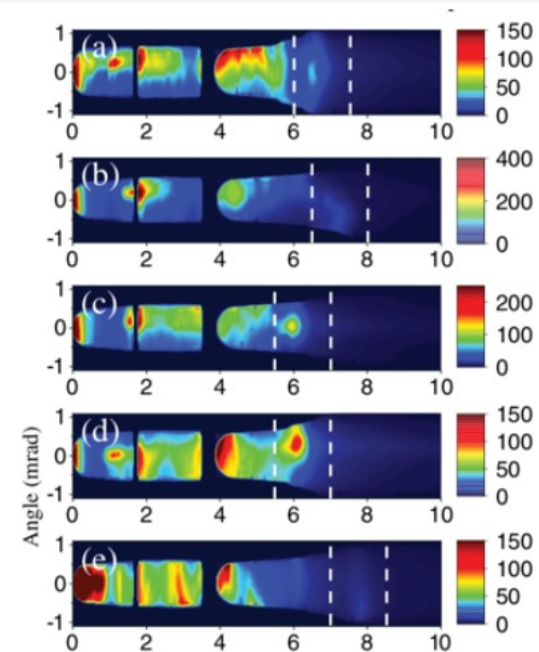
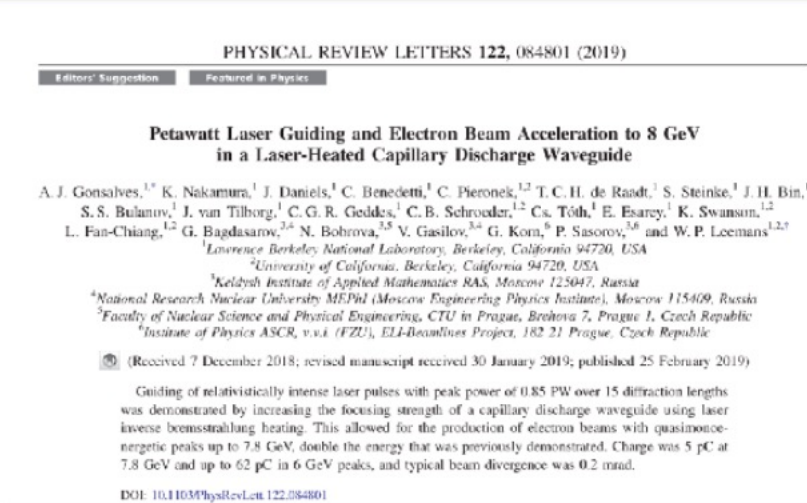


- 4 GeV
- $n_e = 7 \times 10^{17} \text{ cm}^{-3}$, 9 cm capillary discharge waveguide
- $P = 300 \text{ TW}$ “Bella” at LBNL

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

Some experimental results

Experiments at the energy frontier: 2019

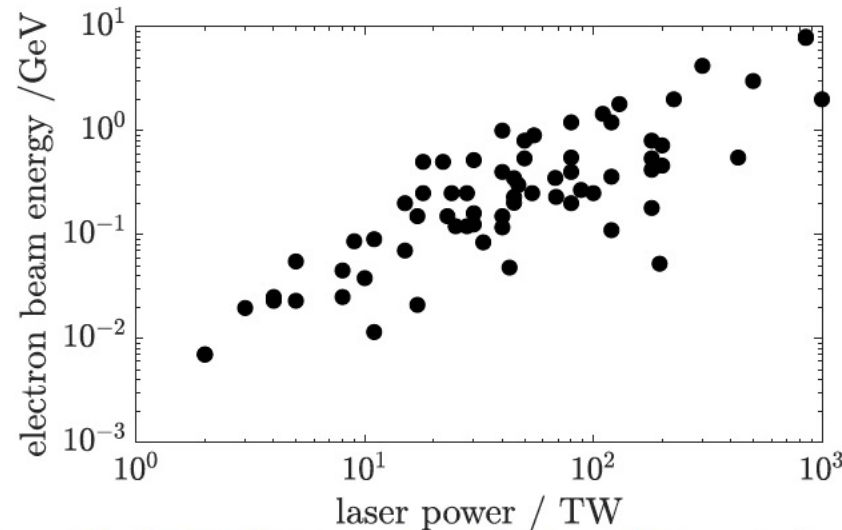


- 7.8 GeV
- $n_e = 7 \times 10^{17} \text{ cm}^{-3}$, 9 cm capillary discharge waveguide
- $P = 850 \text{ TW}$ “Bella” at LBNL

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

Some experimental results

But science isn't about collecting World Records.... Can we extract some physics from the data trends?

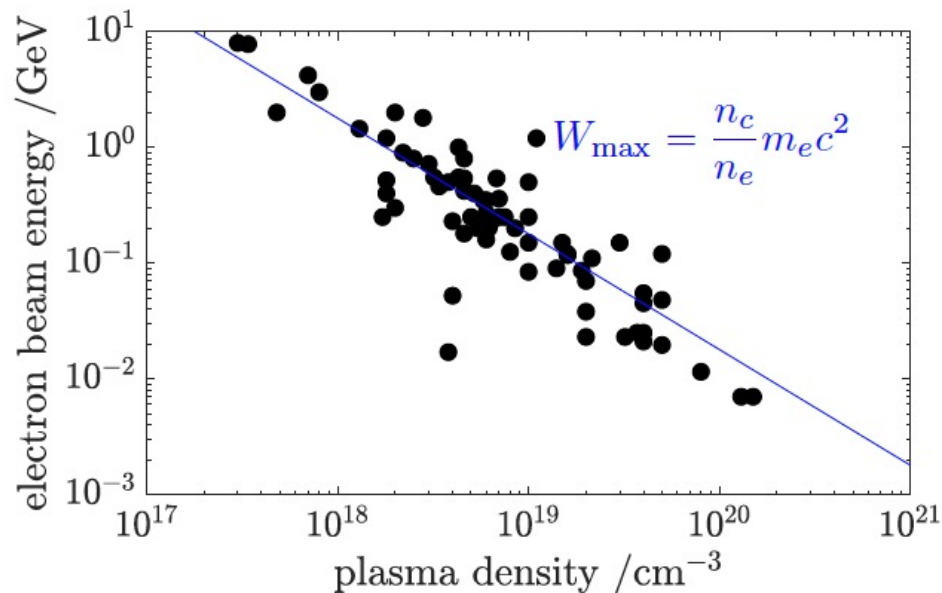


- Collection of data from a variety of experiments
 - (not just the record breakers, but probably the highest beam each experiment was capable of producing)
 - Trend is: higher laser power = higher electron energy
 - What is physics behind this?

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

Some experimental results

Electron energy is limited by dephasing
– move to lower densities



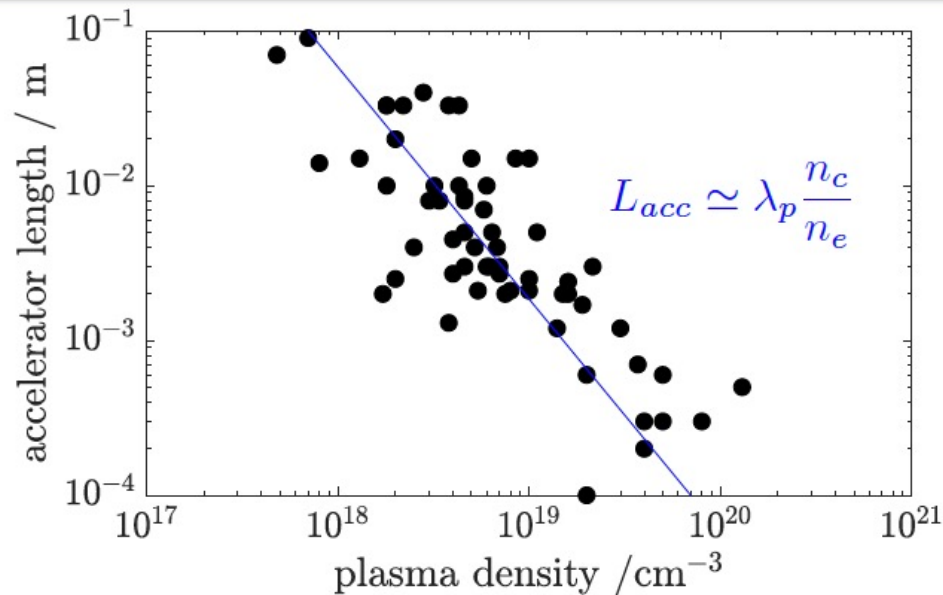
- Beam energy, W_{max} , is inversely proportional to plasma density as expected for dephasing

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

Some experimental results

Electron energy is limited by dephasing

– move to lower densities and longer accelerators

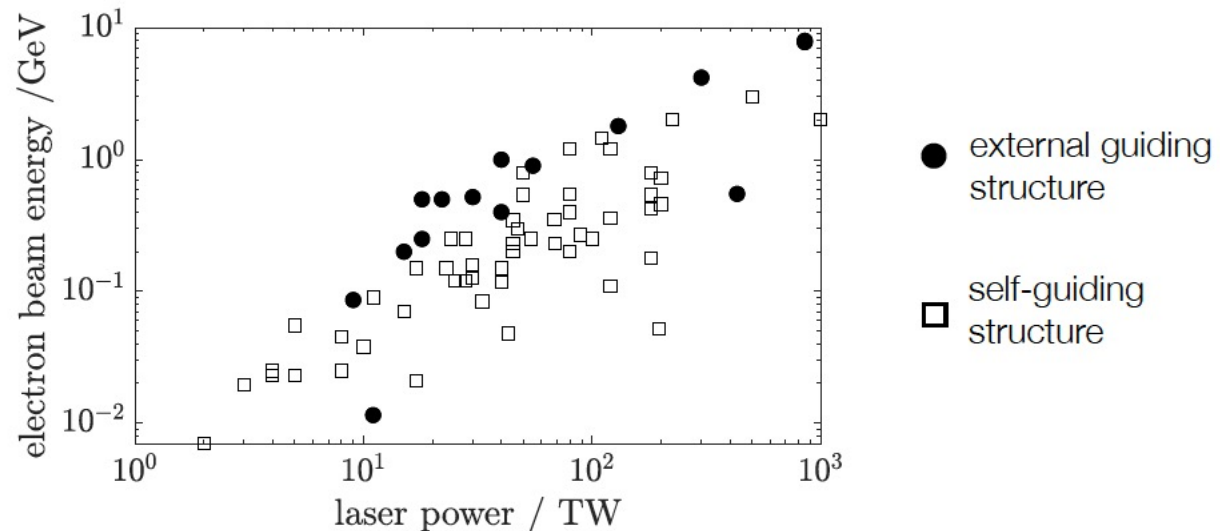


- Accelerator length increases for lower density experiments
 - data lies close to dephasing length (even for simplest linear regime expression)

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

Some experimental results

To guide or not to guide?

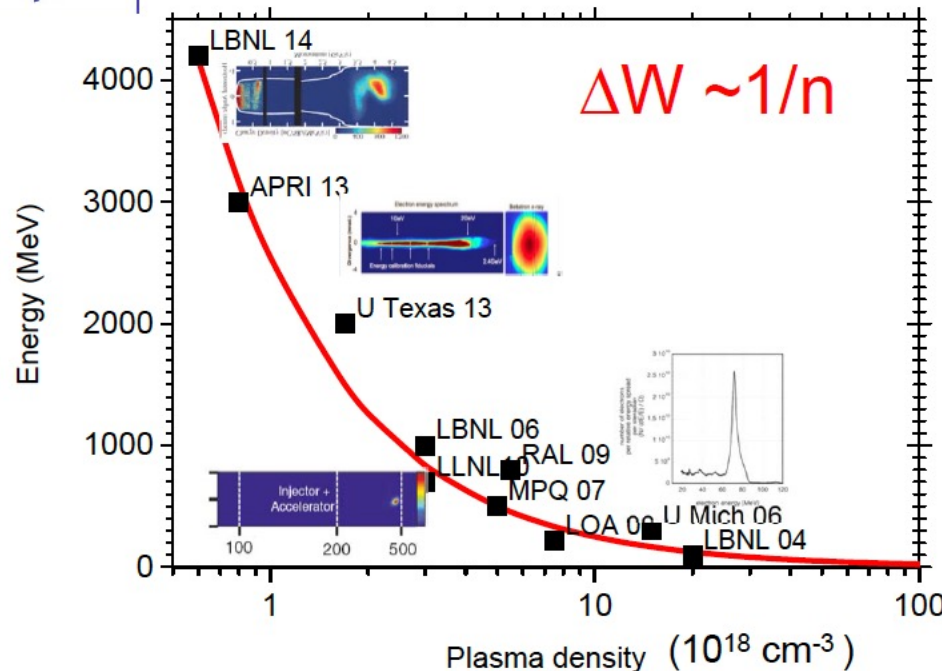


- Data shows that experiments in pre-formed plasma structures are “best” performers
 - i.e. for a given laser power the highest energy beams produced come from guided experiments
 - one (common) explanation is that guiding structure is less lossy

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

Dephasing length

Energy gain is large at low plasma density over a long distance



Non Linear regime with injection of plasma electrons

Energies above GeV reached for PW laser power: U Texas 13, APRI 13: 2 gaz jets

LBNSL 14 also includes channel guiding

- ➡ Energy increases for lower plasma density
- ➡ At low enough density, self-injection stops, additional laser power or external injection should be used

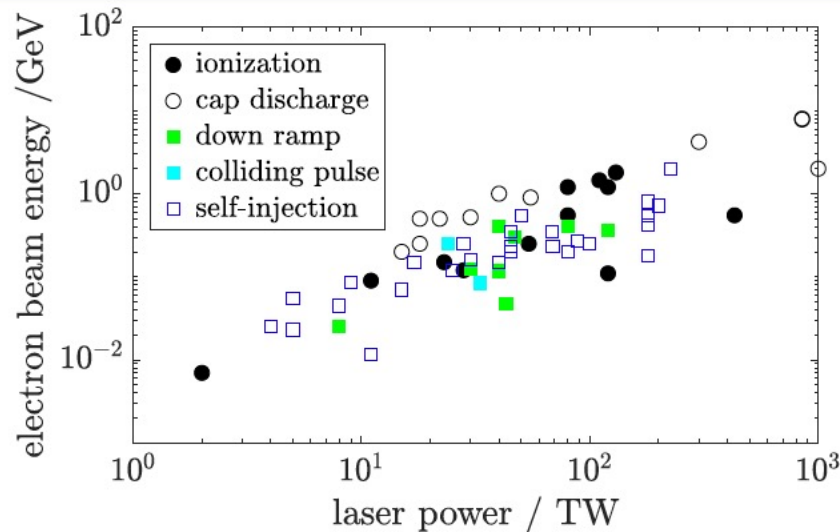
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Courtesy of Brigitte Cros, CAS 2019
Plasma acceleration

Some experimental results

To inject or not to inject?

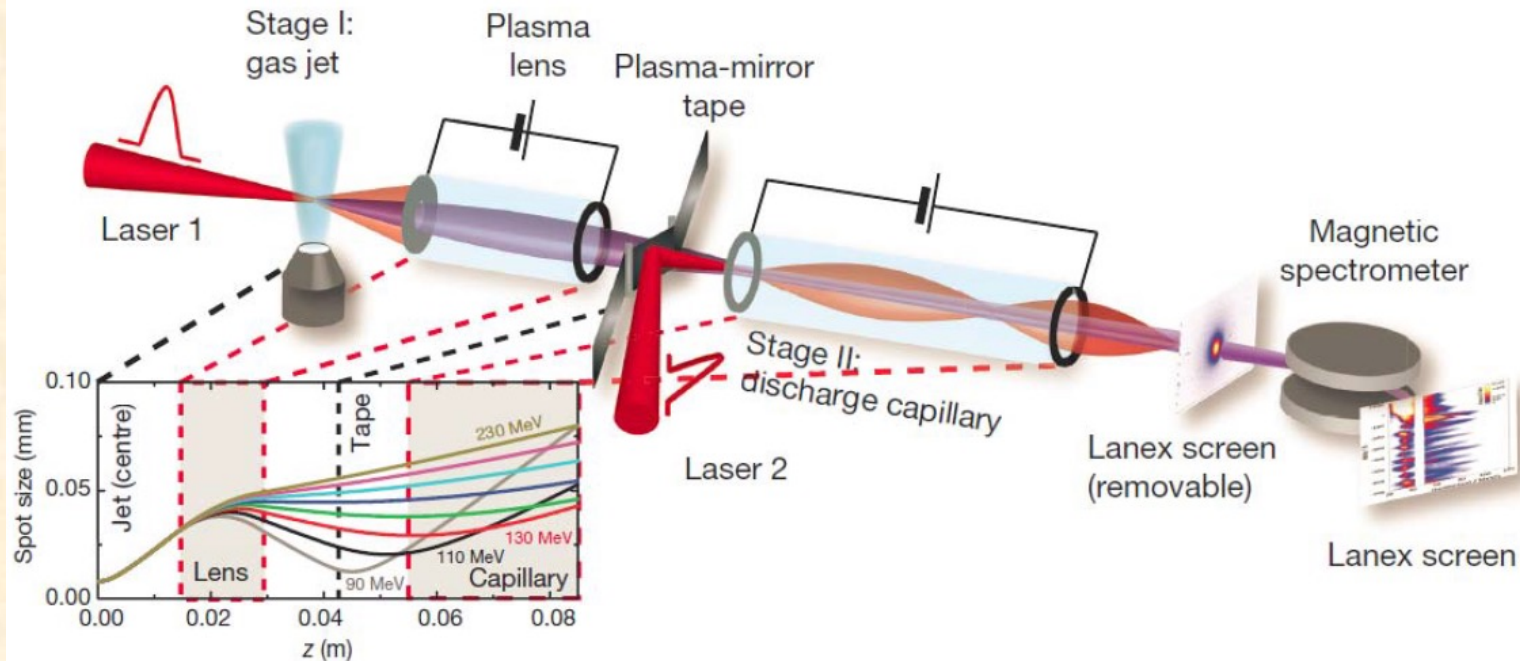


- some ionisation injection experiments also lie at upper edge of distribution
 - data too noisy for a definitive answer, but an interesting research question

Courtesy of Stuart Mangles, CAS 2019
Plasma acceleration

Multi-stage

Coupling an electron source to a plasma accelerator



S. Steinke et al., Nature 2016

B. Cros, CAS HGWA Sesimbra, March 2019



Courtesy of Brigitte Cros, CAS 2019
Plasma acceleration

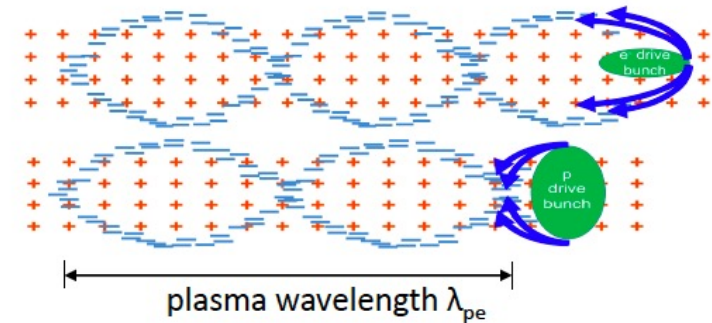
BEAM DRIVEN PLASMA ACCELERATION

Beam driven plasma acceleration

Plasma Wakefield Acceleration

Different ways to excite the wakes - most commonly used:

- Laser bunches, Electron beams, Protons bunches



A plasma of density n_{pe} is characterized by the plasma frequency

$$\omega_{pe} = \sqrt{\frac{n_{pe} e^2}{m_e \epsilon_0}} \Rightarrow \frac{c}{\omega_{pe}} \dots \text{unit of plasma [m]} \quad k_{pe} = \frac{\omega_{pe}}{c}$$

$$\text{Example: } n_{pe} = 7 \times 10^{14} \text{ cm}^{-3} \text{ (AWAKE)} \Rightarrow \omega_{pe} = 1.25 \times 10^{12} \text{ rad/s} \Rightarrow \frac{c}{\omega_{pe}} = 0.2 \text{ mm} \Rightarrow k_{pe} = 5 \text{ mm}^{-1}$$

This translates into a wavelength of the plasma oscillation

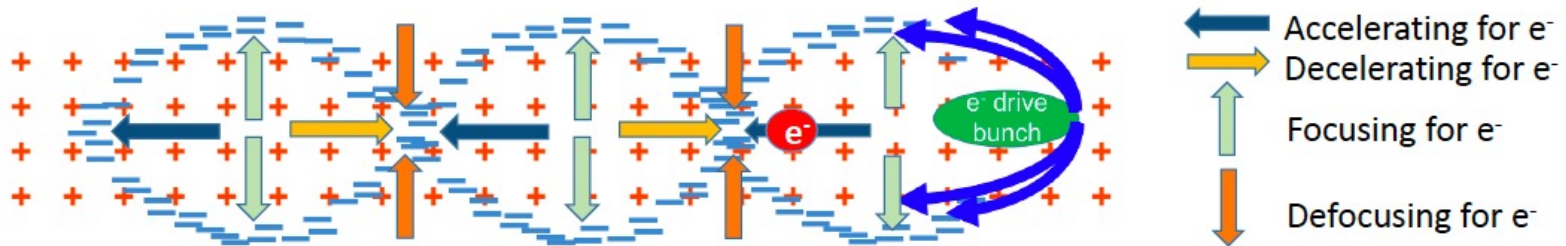
$$\lambda_{pe} = 2\pi \frac{c}{\omega_{pe}} \rightarrow \lambda_{pe} \approx 1 \text{ mm} \sqrt{\frac{10^{15} \text{ cm}^{-3}}{n_{pe}}}$$

$$\lambda_{pe} = 1.2 \text{ mm} \rightarrow \text{Cavities with mm size!}$$

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Beam driven plasma acceleration

Wakefields



How strong can the fields be?

- The plasma oscillation leads to a longitudinal accelerating field. The maximum accelerating field (wave-breaking field) is:
- The ion channel left on-axis, where the beam passes, induces an **ultra-strong focusing field**:

$$e E_{WB} = 96 \frac{V}{m} \sqrt{\frac{n_{pe}}{cm^{-3}}}$$

$$g = 960 \pi \frac{n_{pe}}{10^{14} cm^{-3}} \frac{T}{m}$$

Example: $n_{pe} = 7 \times 10^{14} cm^{-3}$ (AWAKE) $\rightarrow e E_{WB} = 2.5 GV/m \rightarrow g = 21 kT/m$
Example: $n_{pe} = 7 \times 10^{17} cm^{-3}$ $\rightarrow e E_{WB} = 80 GV/m \rightarrow g = 21 MT/m$

Beam driven plasma acceleration

Record Acceleration, at SLAC: 42 GeV

Final Focus Test Beam Facility, **FFTB** at SLAC

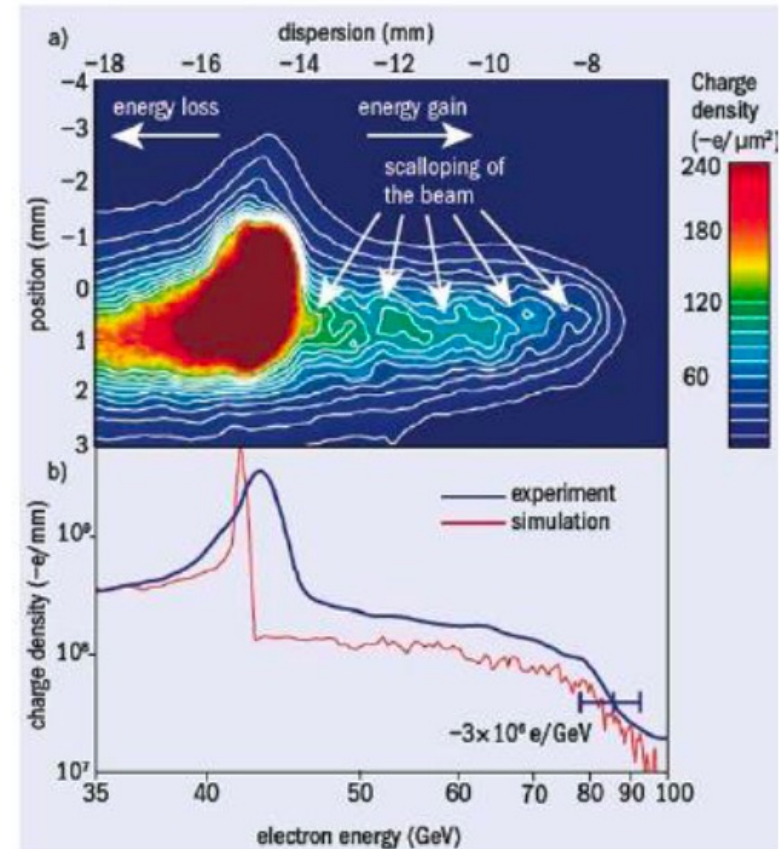
I. Blumenfeld et al, Nature 455, p 741 (2007)

Gaussian electron beam with 42 GeV, 3nC @ 10 Hz, $\sigma_x = 10\mu\text{m}$, 50 fs

85cm Lithium vapour source, $2.7 \times 10^{17} \text{cm}^{-3}$

→ Accelerated electrons from 42 GeV to 85 GeV in 85 cm.

→ Reached accelerating gradient of **52 GeV/m**



Courtesy of Edda Gschwendtner, CAS 2019
Plasma acceleration

Beam driven plasma acceleration

SLAC – FACET

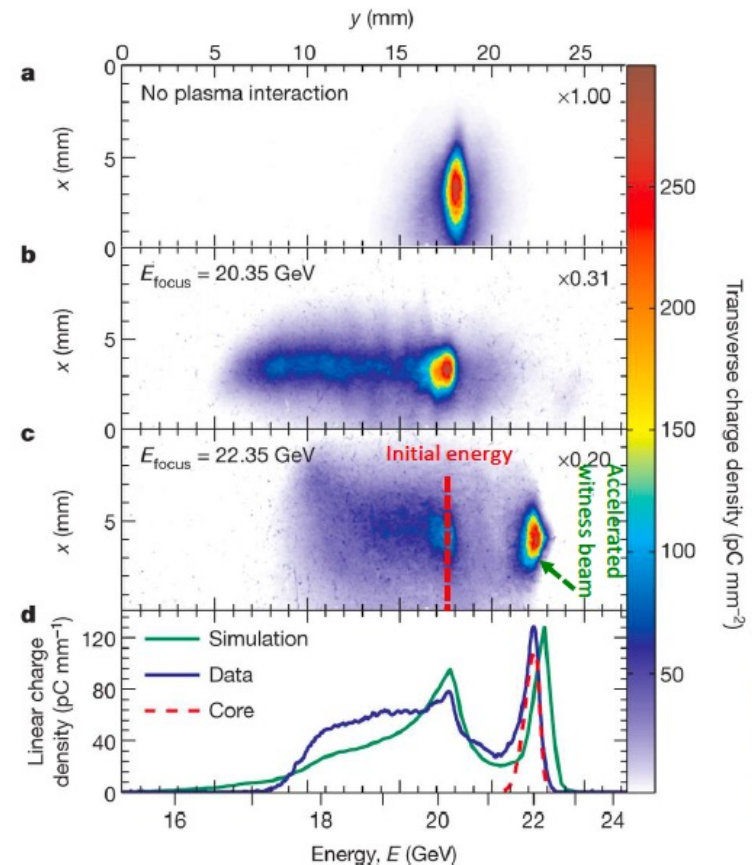
High-Efficiency acceleration of an electron beam in a plasmas wakefield accelerator, 2014

M. Litos et al., doi, Nature, 6 Nov 2014, 10.1038/nature 13882

- Laser ionized Lithium vapour plasma cell:
 - 36 cm long, Density: $5 \times 10^{16} \text{ cm}^{-3}$, $\lambda_{\pi} = 200 \text{ }\mu\text{m}$
- Drive and witness beam:
 - 20.35 GeV, D and W separated by $160 \text{ }\mu\text{m}$
 - 1.02nC (D), 0.78nC (W)

First demonstration of a high-efficiency, low energy-spread plasma wakefield acceleration experiment:

- 70 pC of charge accelerated
- 2 GeV energy gain
- 5 GeV/m gradient
- Up to 30% transfer efficiency
- ~2% energy spread



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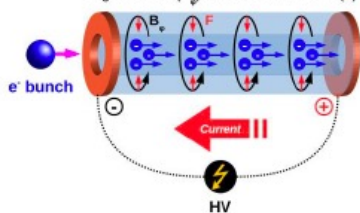
Courtesy of Edda Gschwendtner, CAS 2019
Plasma acceleration

Plasma lens

SPARCLAB, Plasma Lens Experiment

Plasma Lens

Magnetic Field (B_z) vs Force on electrons (F)



Beam focusing by azimuthal magnetic field generated by the discharge current density

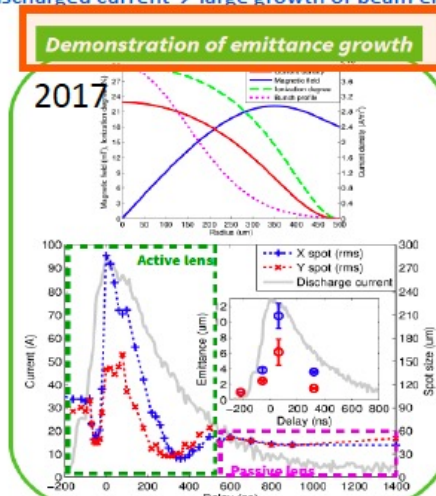
$$B_\phi(r) = \frac{\mu_0}{r} \int_0^r J(r') r' dr'$$

Experiment:

127MeV, 50pC, $\sigma_t=1.3\text{ps}$, $\epsilon_N \sim 1\text{ mm mrad}$,
 $\sigma_x = 110\mu\text{m}$.

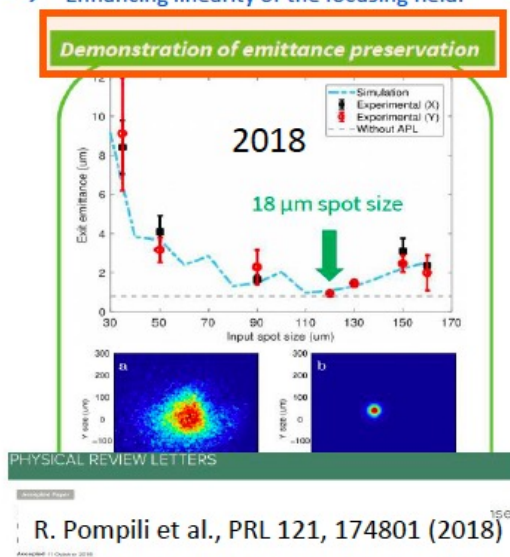
Capillary discharge plasma cell, 3cm,
 $R_0=500\mu\text{m}$, $I=100\text{A}$, $V=20\text{kV}$, H_2 gas, $n_e = 9 \times 10^{16} \text{cm}^{-3}$,

→ Focusing is non-linear due to non-uniformity of the discharged current → large growth of beam emittance



R. Pompili et al., Applied Physics Letters 110.10 (2017):104101
 A. Marocchino et al., Applied Physics Letters 111.18(2017):184101

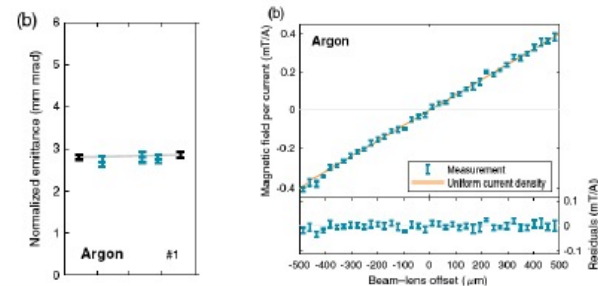
→ Change plasma discharge
 → Enhancing linearity of the focusing field.



R. Pompili et al., PRL 121, 174801 (2018)



C. Lindstroem et al., Emittance Preservation in Aberration-Free Active Plasma Lens, PRL 121, 194801 (2018)



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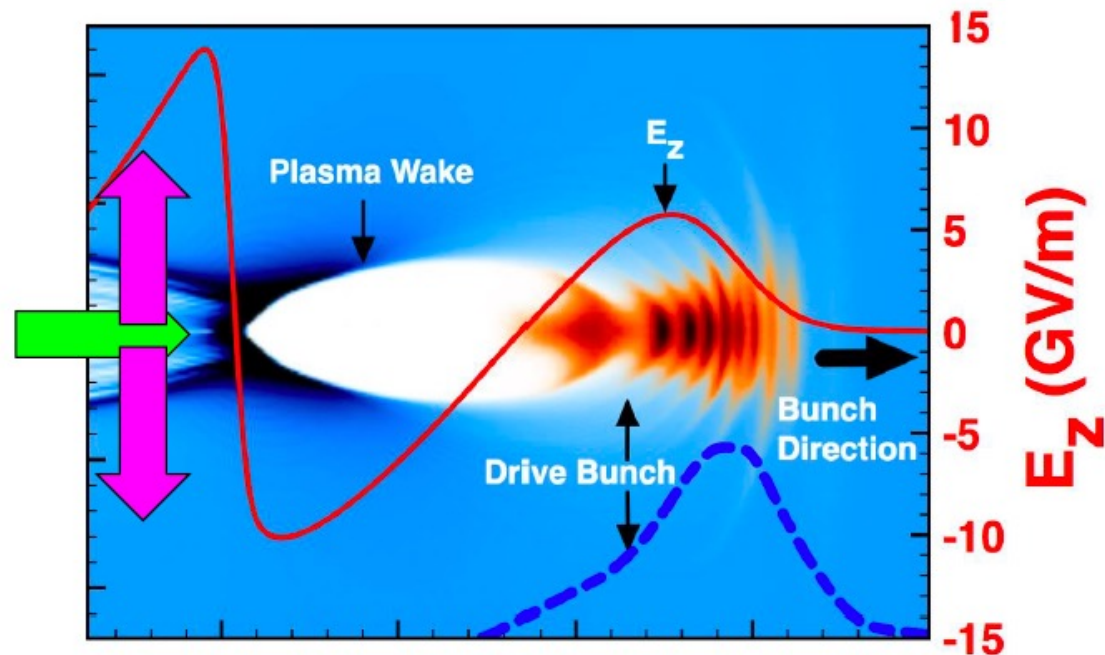
POSITRON ACCELERATION

Positron acceleration

Positron Acceleration

- Interested in using positrons for high energy linear colliders:
 - Parameters for positrons: **high energy, high charge, low emittance.**

Electron-driven blowout wakes:



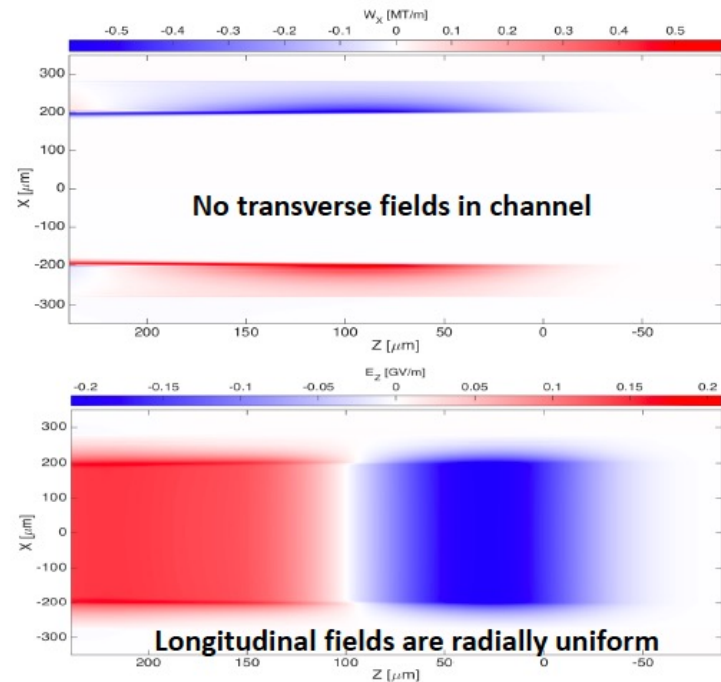
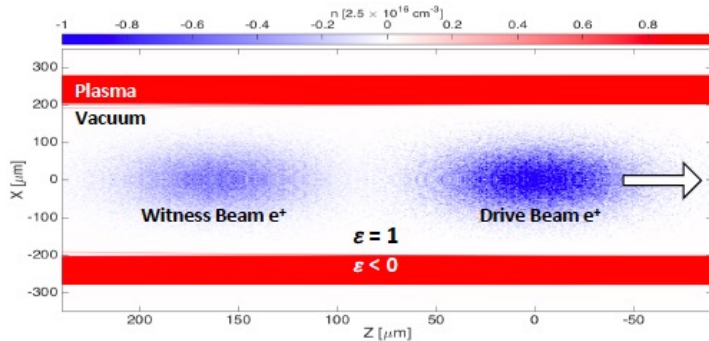
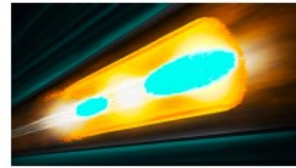
But the field is **defocusing** in this region.

Courtesy of Edda Gschwendtner, CAS 2019
Plasma acceleration

Positron acceleration

Positron Acceleration in Hollow Channel at FACET

- There is no plasma on-axis, and therefore no complicated forces from plasma electrons streaming through the beam.
- Treat the plasma as dielectric

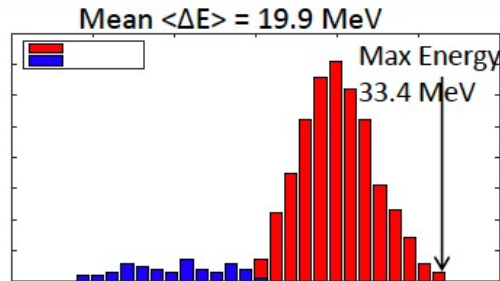


Courtesy of Edda Gschwendtner, CAS 2019
Plasma acceleration

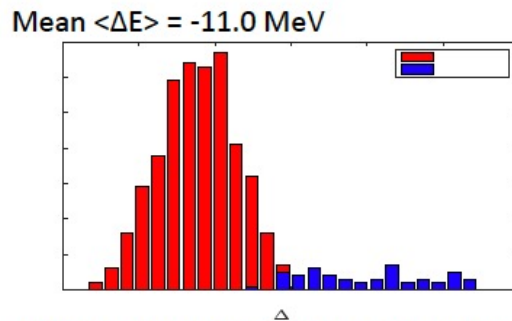
Positron acceleration

Positron Acceleration in Hollow Channel at FACET, 2016, 2018

First Demonstration of Acceleration in Hollow channel



Witness beam gains energy from the wake.



Drive beam transfers energy to witness beam.

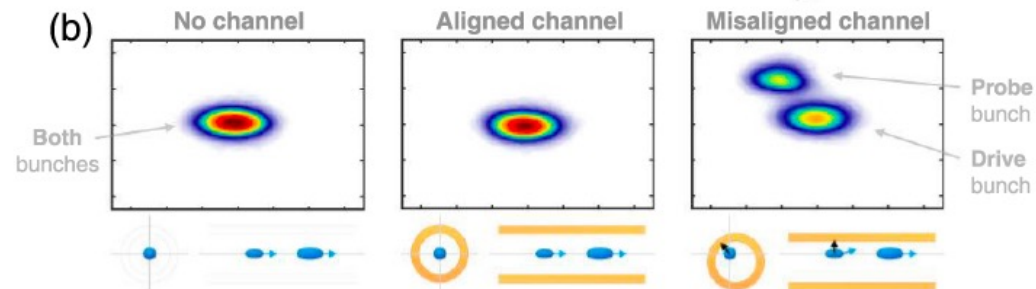
S. Gessner et. al. *Nat. Comm.* 7, 11785 (2016)

Measurement of transverse wakefields in hollow channel

→ the result agrees with theoretical calculation:

$$10^6 \text{ V}/(\text{pC m mm})$$

Or about 10,000 times stronger than the wakefields in CLIC!



C. A. Lindstrøm et. al. *Phys. Rev. Lett.* 120 124802 (2018).

PROTON DRIVEN PLASMA ACCELERATION

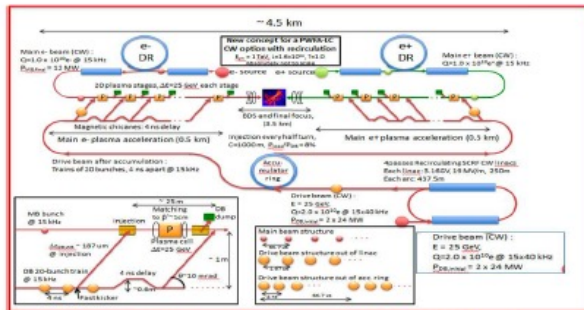
Protons as a driver

Energy Budget for High Energy Plasma Wakefield Accelerators

Lasers: ~40 J/pulse
Electron drive beam: 30 J/bunch
Proton drive beam: SPS 19kJ/pulse, LHC 300kJ/bunch

Electrons: 10^{10} particles @ 1 TeV ~few kJ

- **Electron/laser driven PWA:** need several stages, and challenging wrt to relative timing, tolerances, matching, etc...
 - effective gradient reduced because of long sections between accelerating elements....



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Protons as a driver

Seeded Self-Modulation of the Proton Beam

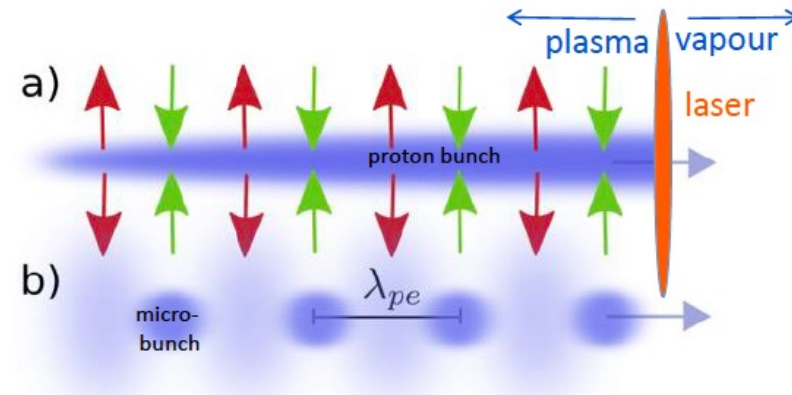
In order to create plasma wakefields efficiently, the drive bunch length has to be in the order of the plasma wavelength.

CERN SPS proton bunch: very long! ($\sigma_z = 12$ cm) \rightarrow much longer than plasma wavelength ($\lambda = 1$ mm)

N. Kumar, A. Pukhov, K. Lotov,
PRL 104, 255003 (2010)

Self-Modulation:

- a) Bunch drives wakefields at the initial seed value when entering plasma.
 - Initial wakefields act back on the proton bunch itself. \rightarrow On-axis dens is modulated. \rightarrow Contribution to the wakefields is $\propto n_b$.
- b) Density modulation on-axis \rightarrow micro-bunches.
 - Micro-bunches separated by plasma wavelength λ_{pe} .
 - drive wakefields resonantly.



\rightarrow Seeded Self-Modulation

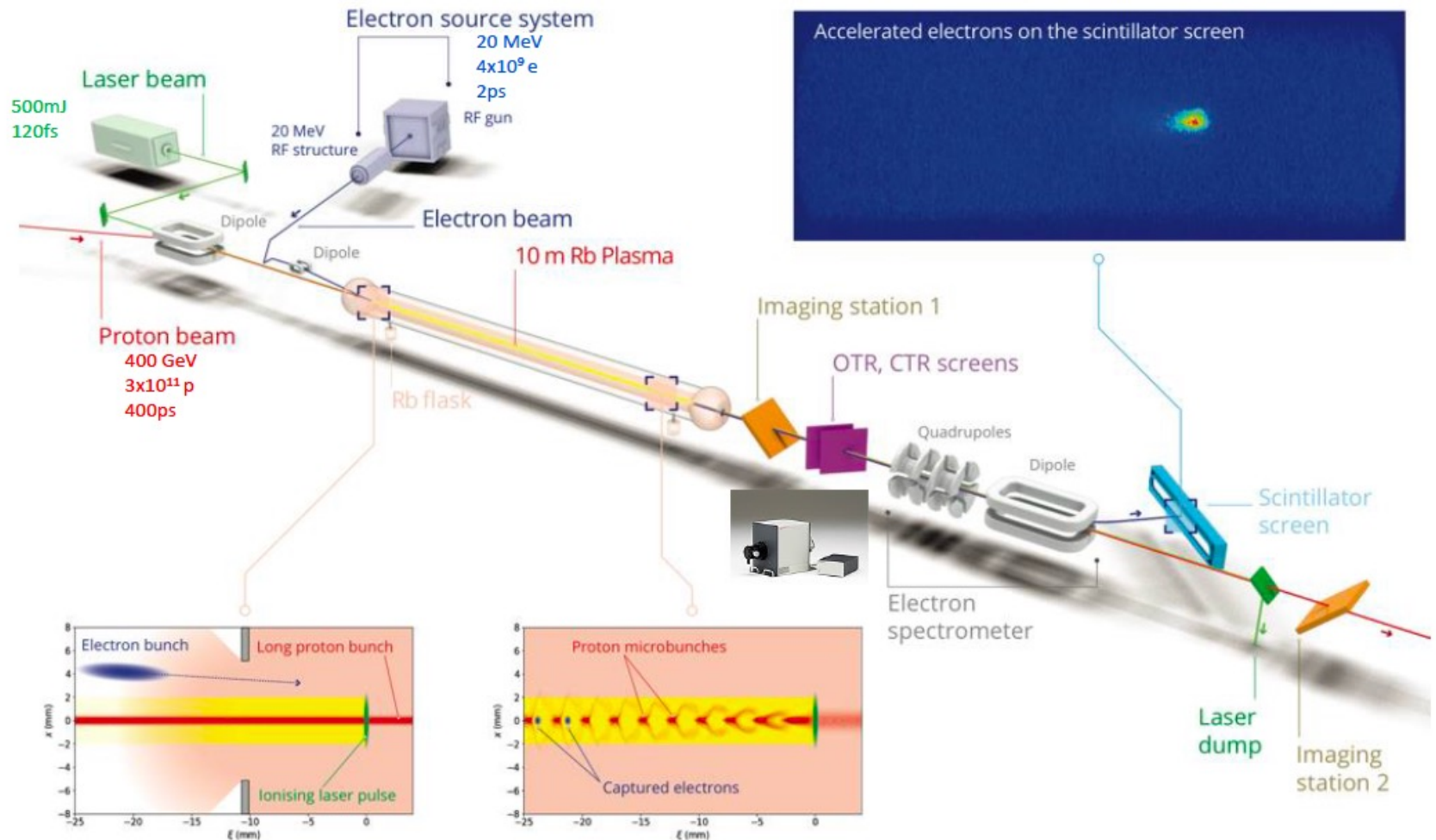
AWAKE: Seeding of the instability by

- Placing a **laser** close to the center of the proton bunch
- Laser ionizes vapour to produce plasma
- Sharp start of beam/plasma interaction
- \rightarrow Seeding with ionization front

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Protons as a driver

AWAKE Experiment

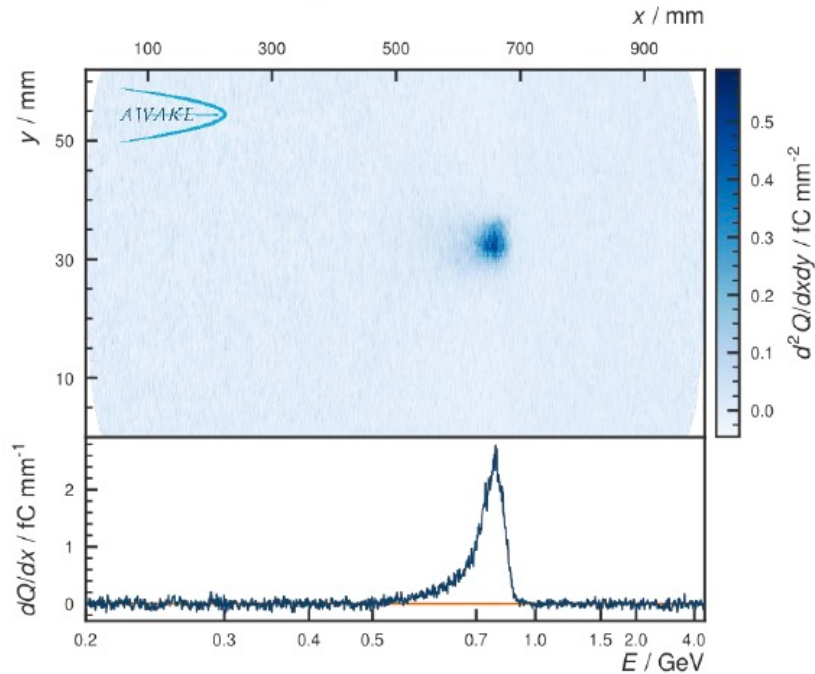


Courtesy of Edda Gschwendtner, CAS 2019
Plasma acceleration

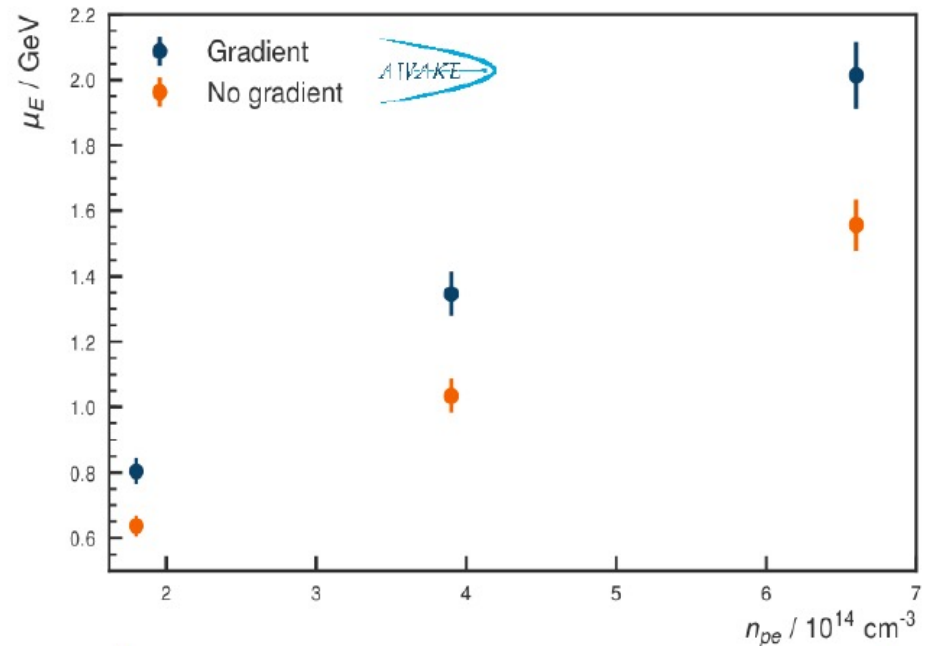
Protons as a driver

Electron Acceleration Results, 2018

Results from May 2018 Run



Event at $n_{pe} = 1.8 \times 10^{14} cm^{-3}$ with 5%/10m density gradient.



→ Acceleration up to 2 GeV has been achieved.

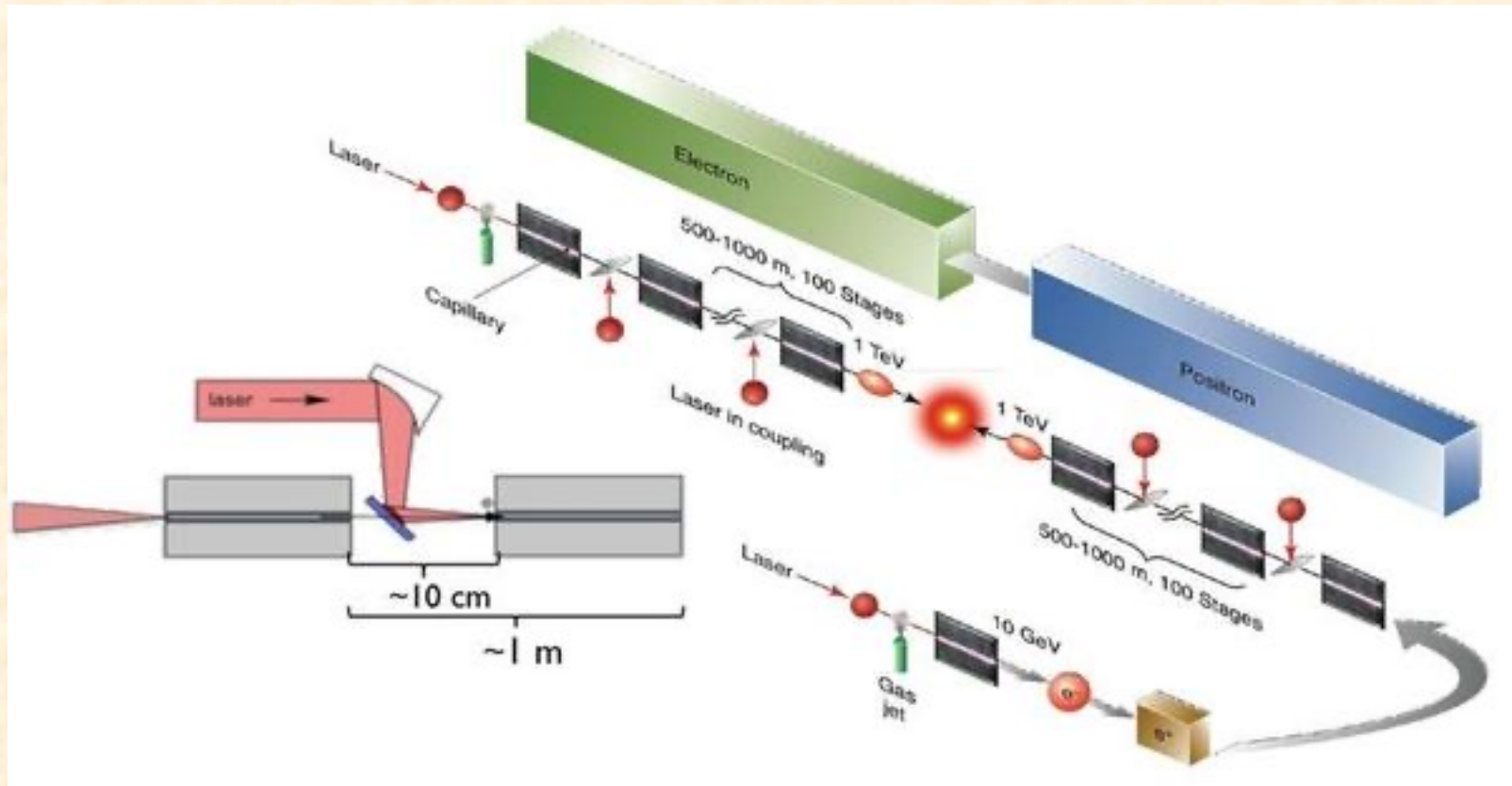
AWAKE Collaboration, Nature, doi:10.1038/s41586-018-0485-4 (2018)

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Courtesy of Edda Gschwendtner, CAS 2019
Plasma acceleration

A PLASMA COLLIDER?

A plasma collider proposal

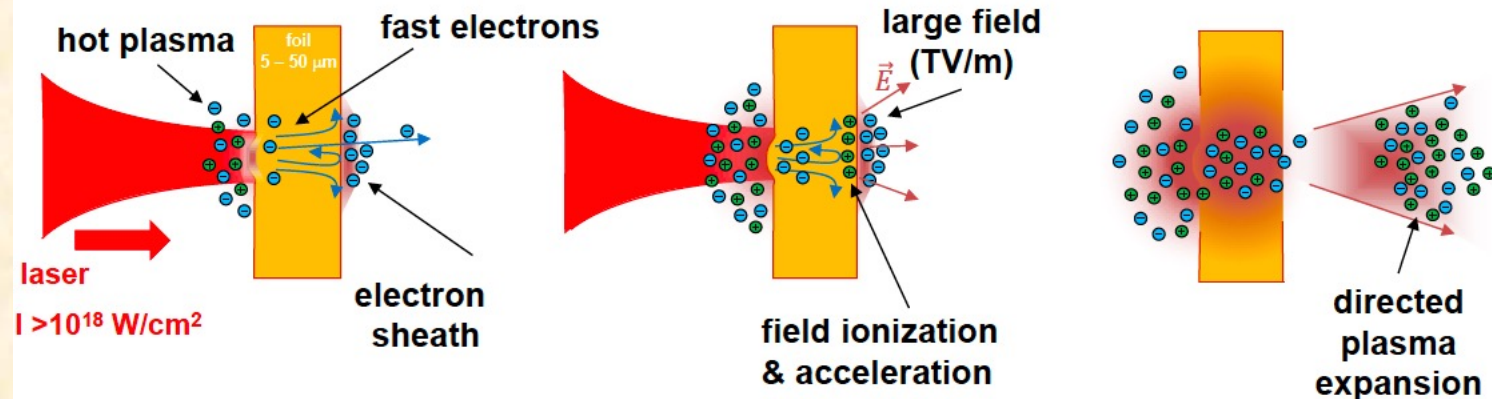


- A concept of plasma collider has been proposed.
<https://physicstoday.scitation.org/doi/10.1063/1.3099645>

ACCELERATION OF IONS

Acceleration of ions

TNSA is the most widely used and robust acceleration scheme



- **intense:** 10^{10} – 10^{13} protons
 - initial bunch duration ≤ 1 ps
 - source size $< 100 \mu\text{m}$
- **ultra-low emittance***
 - $< 0.01 \text{ mm mrad trans.}$
 - $< 10^{-4} \text{ eV s long.}$
- **compact:** MV/ μm

- **divergence:** ≤ 30 deg (half angle)
- **continuous exp. spectrum**
- **disturbed environment**
 - electrons
 - large background: γ , X-rays, EMP

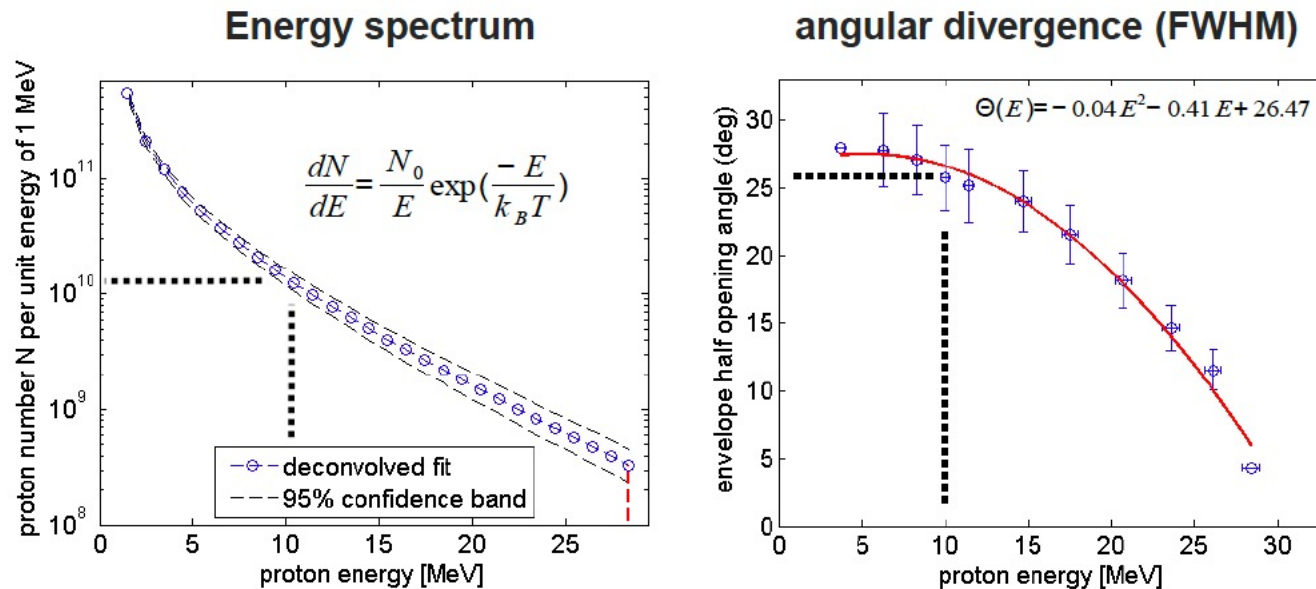
*T. E. Cowan *et al.*, PRL **92**, 204801 (2004)

GSI Helmholtzzentrum für Schwerionenforschung GmbH

Courtesy of Vincent Bagnoud, CAS 2019
Plasma acceleration

Acceleration of ions

Typical properties of TNSA beams exhibit a broad spectrum and large angular divergence



- ♦ detection of full proton beam via RIS* @4cm behind source
- ♦ source size @10MeV: approx. 50 μ m

*F. Nürnberg *et al.*, RSI **80**, 033301

GSI Helmholtzzentrum für Schwerionenforschung GmbH

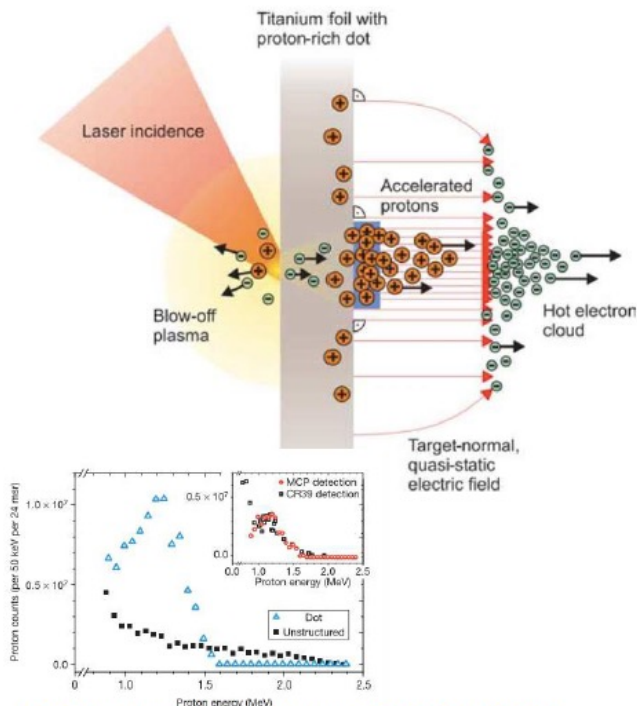
5

Courtesy of Vincent Bagnoud, CAS 2019
Plasma acceleration

Acceleration of ions

Ion acceleration mechanisms:
Small energy spread using TNSA?

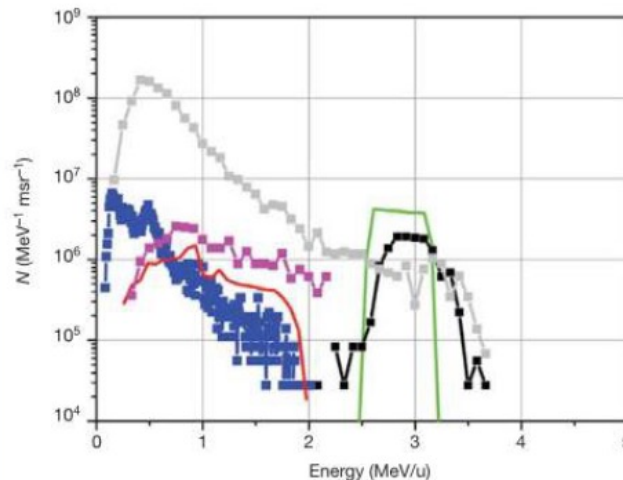
Structured targets (CH microdot)



H Schworer, et al, Nature, 439, 445 (2006);
APL Robinson and P Gibbon, PRE, 75, 015401 (2007)

Complex target preparation:

“an ultrathin layer of graphitic carbon, formed from catalytic decomposition of adsorbed hydrocarbon impurities on a 20 mm palladium foil.”



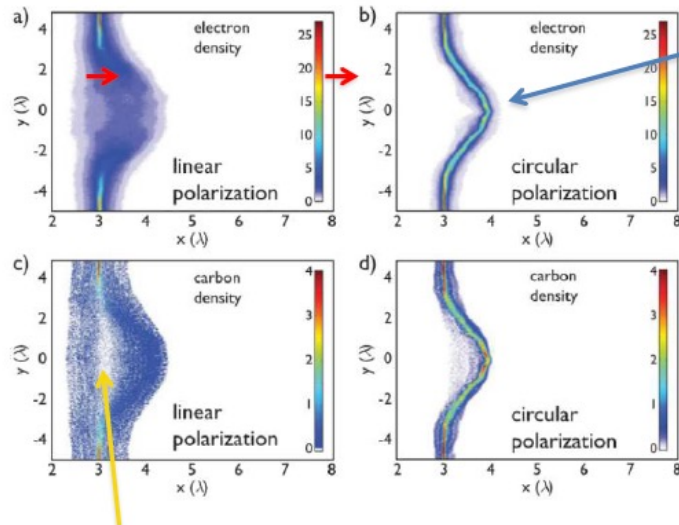
BM Hegelich, et al, Nature, 439, 441 (2006)

Courtesy of Louise Willingale, CAS 2019
Plasma acceleration

Acceleration of ions

Advanced ion acceleration mechanisms: Radiation Pressure Acceleration (RPA)

A Henig, et al, PRL, 103, 245003 (2009)



Linear polarization heats electrons strongly and explodes foil, preventing the “light-sail” from forming – TNSA instead.

Laser light pressure pushes entire electron volume of a very thin foil forward forming the acceleration field:

“Light Sail” regime

The ions follow the electrons – all experience same field \rightarrow same final energy.

- ✓ Excellent ion energy scaling with laser intensity
- ✓ Excellent energy conversion efficiency
- ✓ Quasi-monoenergetic acceleration

- ✗ Very thin targets difficult to handle
- ✗ Requires challenging laser parameters:
 - Very small laser pre-pulse
 - Circular polarization
 - Large focal spot, increases the laser energy required
- ✗ Experimental demonstrations have been so far disappointing

Esirkepov, et al, PRL, 92, 175003 (2004)

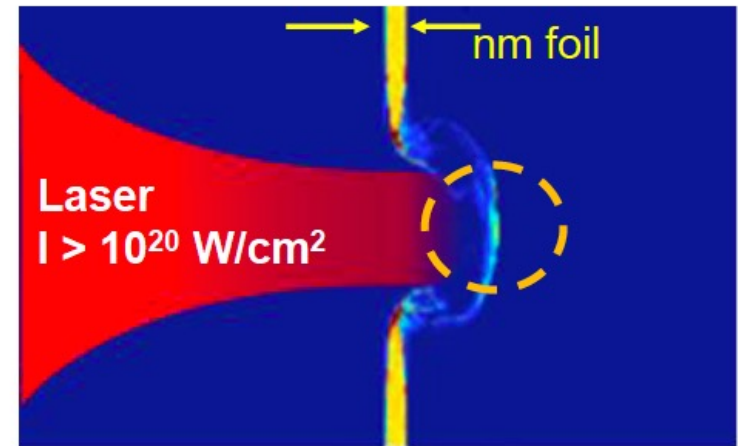
Courtesy of Louise Willingale, CAS 2019
Plasma acceleration

Acceleration of ions

RPA and BOA/RITA require ultrathin targets



- “advanced schemes” rely on a direct acceleration
- Very hard experimental conditions are necessary
 - thin foils are necessary (typically < skin depth = 10's nm)
 - electrons should remain cold – circularly polarized light is necessary
 - ultra-clean temporal profile of the laser pulse
- performance of simulations never confirmed experimentally

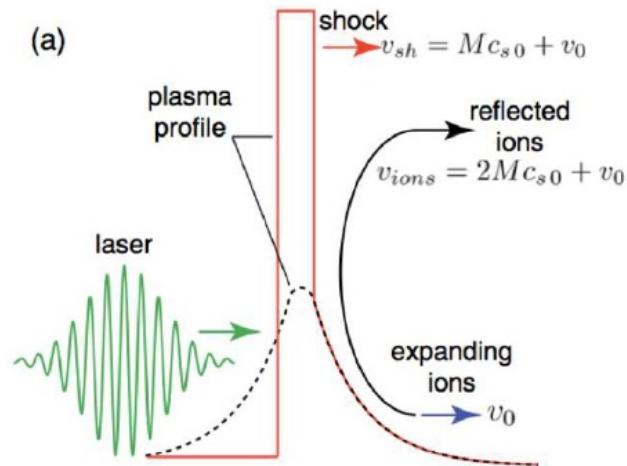


* adapted from Robinson

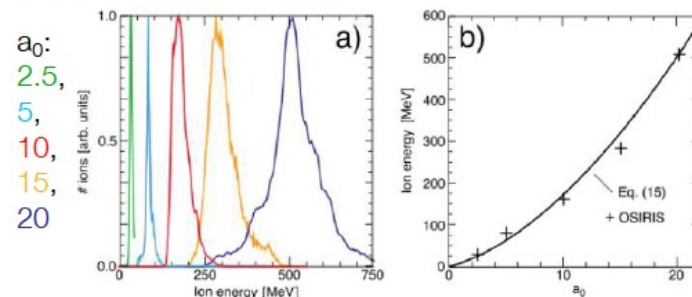
Courtesy of Vincent Bagnoud, CAS 2019
Plasma acceleration

Acceleration of ions

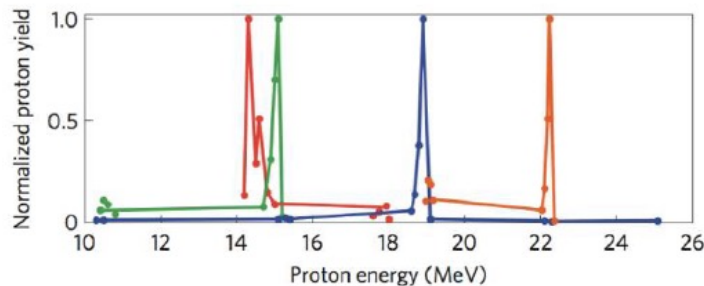
Advanced ion acceleration mechanisms: Shock acceleration



Very promising theoretical energy scaling with a_0 :



Demonstration of quasi-monoenergetic proton spectra using CO₂ ($\lambda = 10 \mu\text{m}$) lasers:



Laser	λ	n_c	a_0
CO ₂	10 μm	10^{19} cm^{-3}	2
Glass	1.053 μm	10^{21} cm^{-3}	20
Ti:Sapph	800 nm	$1.1 \times 10^{21} \text{ cm}^{-3}$	50

D Haberberger, et al, Nature Physics, 8, 95 (2012);
F Fiuza, et al, PRL, 109, 215001 (2012);
F Fiuza, et al, Phys Plas, 20, 056304 (2013).

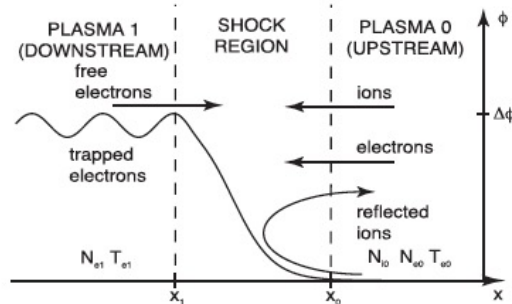
Courtesy of Louise Willingale, CAS 2019
Plasma acceleration

Acceleration of ions

Advanced ion acceleration mechanisms: Shock acceleration

Shock formation requires a high plasma electron temperature, T_{e1} .

F Fiuza, et al, Phys Plas, 20, 056304 (2013)



$$M_{cr} = \sqrt{2 \frac{T_{e1}}{T_{e0}} \left(\frac{1 + \mu_{e0}}{\frac{N_{e1}}{N_{e0}} \left(1 - \mu_{e0} \frac{T_{e0}}{T_{e1}} \right)} + 1 \right)}$$

$$\mu_{e0} = \frac{m_e c^2}{k_B T_{e0}}$$

This requires strong laser absorption and places restrictions on the target size and scalelengths for optimum acceleration.

- ✓ Excellent ion energy scaling with laser intensity
- ✓ Quasi-monoenergetic acceleration
- ✓ Gas-jet useful for high-rep rate & low debris
- ✓ Experimentally demonstrated
- ✗ Requires challenging target parameters:
 - Very-high density gas jet / prepared target
 - Relativistic Transparency increases density requirement – even more difficult
 - Carefully designed density profile needed
- ✗ Large focal spot needed, increases the laser energy required
- ✗ Instabilities not studied

Courtesy of Louise Willingale, CAS 2019

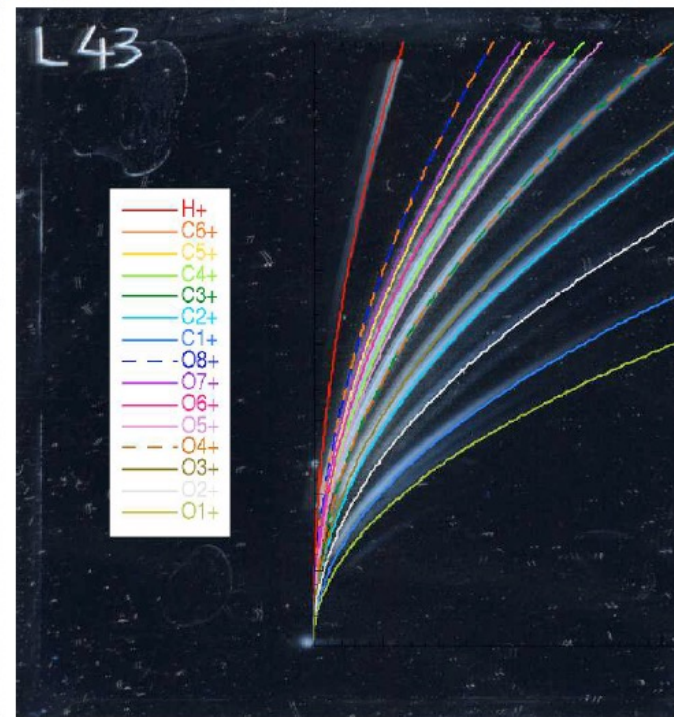
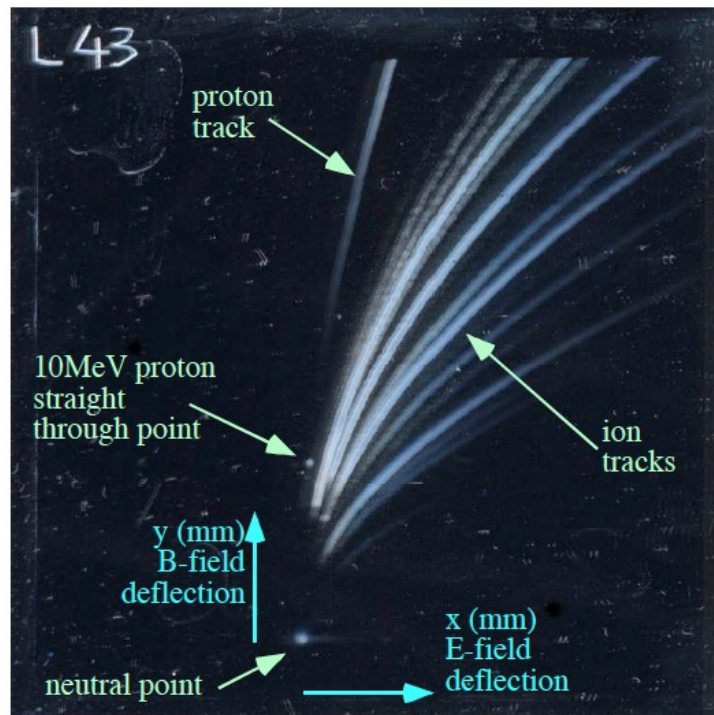
Plasma acceleration

Acceleration of ions

Proton and ion diagnostics: Energy spectra Thomson Parabola Spectrometer

Assuming $v \ll c$, the kinetic energy of the ion, $E_{ion} = \frac{1}{2}Am_u v^2$, is therefore:

$$E_{ion} = \frac{\left[ZeBL_B \left(\frac{1}{2}L_B + l_B \right) \right]^2}{2Am_u} \frac{1}{y^2}$$



Courtesy of Louise Willingale, CAS 2019
Plasma acceleration

Outlook

- Plasma acceleration is a new technique to accelerate particles with a high gradient.
- It is still a research topic.
- Performances have been demonstrated but beam quality still has to be improved.
- Beams are different from conventional accelerators beams.
- Some applications are been considered (FEL, isotope production,...)
- Colliders applications have been discussed but are still far away.

More details

- You can find a large amount of courses on this topics on the website of the CERN accelerator School 2019:
<https://indico.cern.ch/event/759579/>